

Script to analyze the data for the Jarrett, Farwell and Herzberg Plaid design using asreml and asremlPlus

Data available from <https://doi.org/10.25909/13122095>

Initialize

```
library(knitr)
#knitr::spin("FHanal.r")
library(dae)
packageVersion("dae")

## [1] '3.1.38'
library(asreml)

## Loading required package: Matrix
packageVersion("asreml")

## [1] '4.1.0.130'
library(asremlPlus)

## The methods for alldiffs and data.frame do not require asreml
packageVersion("asremlPlus")

## [1] '4.2.32'
library(ggplot2)
library(qqplotr)

##
## Attaching package: 'qqplotr'

## The following objects are masked from 'package:ggplot2':
##       stat_qq_line, StatQqLine
options(width = 100)
opts_chunk$set("tidy" = FALSE, "dev" = "png", "dpi" = 300, fig.path = "figures/",
             "fig.width" = 7.5, "fig.height" = 7.5)
```

A set of colour-blind friendly colours

```
cbPalette <- c("#CC79A7", "#56B4E9", "#009E73", "#E69F00",
                 "#FOE442", "#0072B2", "#D55E00", "#000000")
```

Load data

```
load("plaid.dat.rda")
```

Add factors for heterogeneous variances

```
plaid.dat <- within(plaid.dat,
{
```

```

        MotionsExpress <- fac.combine(list(Motions, Expressiveness),
                                         combine.levels = TRUE)
        WMotionsExpress <- fac.nested(MotionsExpress)
    })
plaid.dat <- with(plaid.dat, plaid.dat[order(MotionsExpress, WMotionsExpress), ])

```

Function to produce diagnostic plots

```

plotDiagnostics <- function(asrtests.obj, dat)
{
  asreml.obj <- asrtests.obj$asreml.obj
  dat <- within(dat,
  {
    res <- residuals(asreml.obj, type="stdCond")
    fit <- fitted(asreml.obj)
  })

  facetting <- list(facet_grid(rows = vars(Expressiveness), cols = vars(Motions)),
                     aes(colour=Trainings),
                     scale_colour_manual(values = cbPalette[3:4]))

  resfitplt <- ggplot(data=dat, aes_string(y="res", x="fit")) +
    labs(x = "Fitted values",
         y = "Standardized residuals") +
    geom_point(na.rm = TRUE, alpha=0.75, size=1.25) +
    geom_hline(yintercept=0, linetype = "solid", alpha=0.3) +
    geom_hline(yintercept=c(-3,3), colour = "maroon") +
    theme_bw() +
    theme(strip.text = element_text(size=10, face="bold")) +
    facetting

  qqplt <- ggplot(data=dat, mapping = aes_string(sample="res")) +
    stat_qq_point(alpha=1, size=1) +
    stat_qq_line(alpha=0.75, colour="maroon") + stat_qq_band(bandType = "ts", alpha = 0.2) +
    labs(x = "Theoretical Quantiles",
         y = "Sample Quantiles") +
    geom_hline(yintercept=0, linetype = "dashed", alpha=0.3) +
    geom_vline(xintercept=0, linetype = "dashed", alpha=0.3) +
    theme_bw() +
    theme(strip.text = element_text(size=10, face="bold")) +
    facetting

  print(resfitplt)
  print(qqplt)
  invisible(list(resfitplt = resfitplt, qqplt = qqplt))
}

```

Set asreml options so that a singular variance matrix is allowed and term order is retained

```
asreml.options(ai.sing = TRUE, keep.order = TRUE)
```

Use pstructure from dae to form a marginality matrix for the fixed effects to use in model selection

```
marg.fix <- pstructure(~ Trainings * Motions * Expressiveness, data = plaid.dat)
marg.fix <- marginality(marg.fix)
```

Set up to collect AIC values

```
AIC.tab <- list()
```

Fit model a) with no intertier variances and equal residual variances

```
ma.asr <- asreml(Y ~ Trainings * Motions * Expressiveness,
                    random = ~ Raters + Viewings + Expressiveness:Patients,
                    aom = TRUE, data = plaid.dat)
```

```
## License check Mon Mar 22 16:42:14 2021
## Model fitted using the gamma parameterization.
## ASReml 4.1.0 Mon Mar 22 16:42:15 2021
##          LogLik      Sigma2      DF    wall     cpu
## 1     -1573.378  4.74180  1176 16:42:15  0.0
## 2     -1556.653  4.62557  1176 16:42:15  0.0
## 3     -1539.037  4.49811  1176 16:42:15  0.0
## 4     -1527.011  4.39774  1176 16:42:15  0.0
## 5     -1520.116  4.32943  1176 16:42:15  0.0
## 6     -1517.532  4.29709  1176 16:42:15  0.0
## 7     -1516.781  4.28270  1176 16:42:15  0.0
## 8     -1516.660  4.27707  1176 16:42:15  0.0
## 9     -1516.654  4.27578  1176 16:42:15  0.0
## 10    -1516.654  4.27571  1176 16:42:15  0.0
```

Prepare to use asremlPlus

```
ma.asrt <- as.asrtests(ma.asr, NULL, NULL, IClikelhood = "REML",
                        label = "No intertier variance and equal residual variances")
```

```
## Calculating denominator DF
```

```
(ma.asrt)
```

```
##
## 
## #### Summary of the fitting of the variance parameters
##
##           component   std.error   z.ratio bound %ch
## Viewings          1.4906360  0.89398174  1.667412    P  0
## Expressiveness:Patients 14.4822552  8.81950380  1.642071    P  0
## Raters            0.2777965  0.09155513  3.034199    P  0
## units!R           4.2757080  0.18298341 23.366642    P  0
##
## 
## #### Pseudo-anova table for fixed terms
##
##
```

```

## Wald tests for fixed effects.
## Response: Y
##
##                               Df denDF   F.inc      Pr
## (Intercept)                 1     6 18.910 0.0048
## Trainings                  1    72 11.380 0.0012
## Motions                     1     6 66.020 0.0002
## Trainings:Motions           1 1092 10.220 0.0014
## Expressiveness                1     6  7.355 0.0350
## Trainings:Expressiveness     1 1092  4.769 0.0292
## Motions:Expressiveness       1     6 37.770 0.0009
## Trainings:Motions:Expressiveness 1 1092  8.441 0.0037
##
##
## #### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##                               terms DF denDF   p      AIC      BIC      action
## 1 No intertier variance and equal residual variances 0      4 NA 3041.308 3061.588 Starting model
AIC.tab <- rbind(AIC.tab, infoCriteria(ma.asrt$asreml.obj))

```

Extract standardized residuals and fitted values and produce diagnostic plots

```
plotDiagnostics(ma.asrt, plaid.dat)
```

Get and plot predictions

```

ma.choice <- chooseModel(ma.asrt, terms.marginality = marg.fix,
                           denDF="numeric")

## Calculating denominator DF
chosen.terms <- unlist(ma.choice$sig.terms)
submod <- length(chosen.terms) != 1 && chosen.terms != "Trainings:Motions:Expressiveness"
ma.diffs <- predictPlus(ma.asr, classify = "Trainings:Motions:Expressiveness",
                        error.intervals = "half", meanLSD.type = "factor",
                        LSDby = c("Motions", "Expressiveness"),
                        wald = ma.asrt$wald.tab,
                        Vmatrix = TRUE, tables = "none")

```

If the chosen fixed model is a submodel of T:M:E, transform predictions to conform to the chosen model

```

if (submod)
{
  ma.TMEdiffs <- ma.diffs #save full diffs
  submod.ch <- paste("~", paste(chosen.terms, collapse = " + "))
  cat("\n\n#### Chosen model: ", submod.ch, "\n\n")
  ma.diffs <- linTransform(ma.diffs,
                           linear.transformation = as.formula(submod.ch),
                           classify = "Trainings:Motions:Expressiveness",
                           error.intervals = "half", meanLSD.type = "factor",
                           tables = "none")
}

```

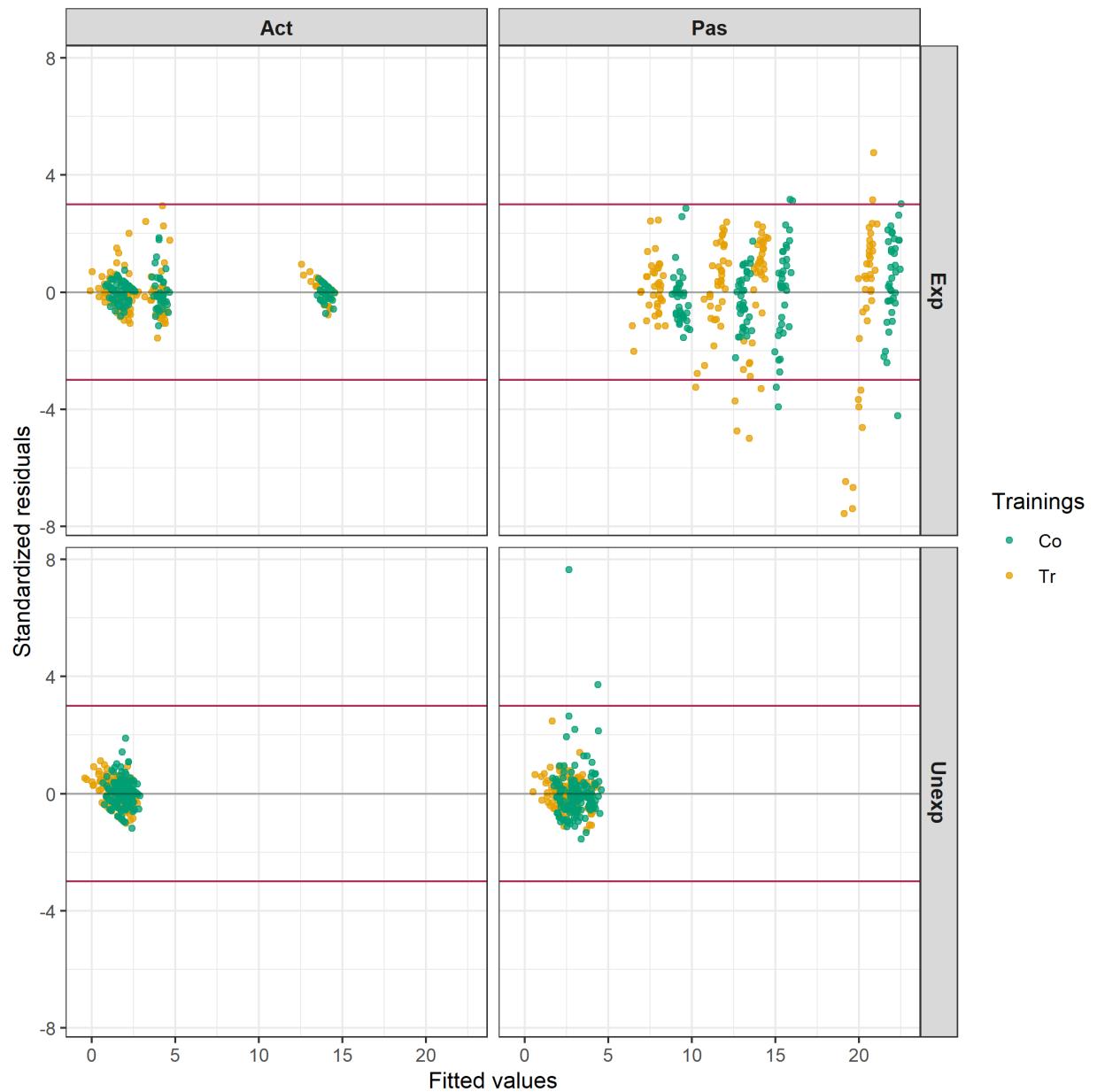


Figure 1: plot of chunk asr_ma

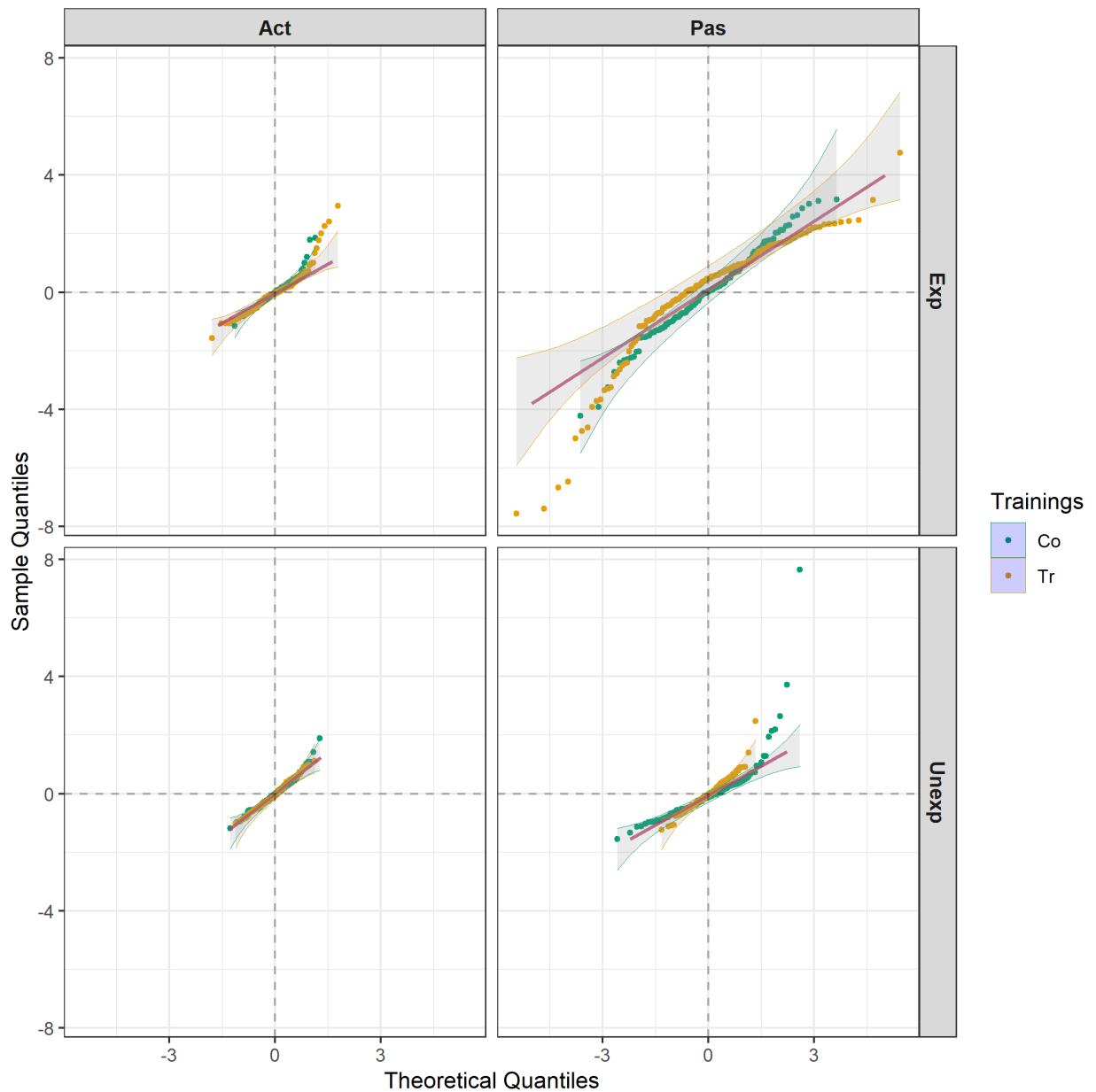


Figure 2: plot of chunk asr_ma

```

        LSDby = c("Motions", "Expressiveness"),
        wald = ma.asrt$wald.tab, tables = "none")
} else
  cat("\n\n##### Chosen model: ~ Trainings:Motions:Expressiveness\n\n")

##
##
## ##### Chosen model: ~ Trainings:Motions:Expressiveness
(ma.diffs$predictions)

##
##
## ##### Predictions
##
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
##   calculated from model terms constructed solely from factors in
##   the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - The ignored set: Raters,Viewings,Patients
##
##
##   Trainings Motions Expressiveness predicted.value standard.error upper.halfLeastSignificant.limit
## 1       Co     Act           Exp    5.370101    2.007392      5.634801
## 2       Co     Act         Unexp   1.790563    2.007392      2.055263
## 3       Co     Pas           Exp   14.982800    2.007392     15.247499
## 4       Co     Pas         Unexp   3.057149    2.007392      3.321848
## 5       Tr     Act           Exp   5.261824    2.007392      5.526524
## 6       Tr     Act         Unexp   1.508846    2.007392      1.773545
## 7       Tr     Pas           Exp  13.407878    2.007392     13.672578
## 8       Tr     Pas         Unexp   2.705541    2.007392      2.970240
##   lower.halfLeastSignificant.limit est.status
## 1             5.105402  Estimable
## 2             1.525864  Estimable
## 3            14.718100  Estimable
## 4            2.792449  Estimable
## 5            4.997125  Estimable
## 6            1.244146  Estimable
## 7           13.143179  Estimable
## 8            2.440841  Estimable

plotPredictions(ma.diffs$predictions, classify = "Trainings:Motions:Expressiveness",
                y = "predicted.value",
                error.intervals = "half", interval.annotate = FALSE,
                ggplotFuncs = list(facet_grid(cols = vars(Expressiveness, Motions)))))

plotPvalues(ma.diffs, factors.per.grid = 2, show.sig = TRUE,
            title = "Initial allocation model, \nequal variances")

```

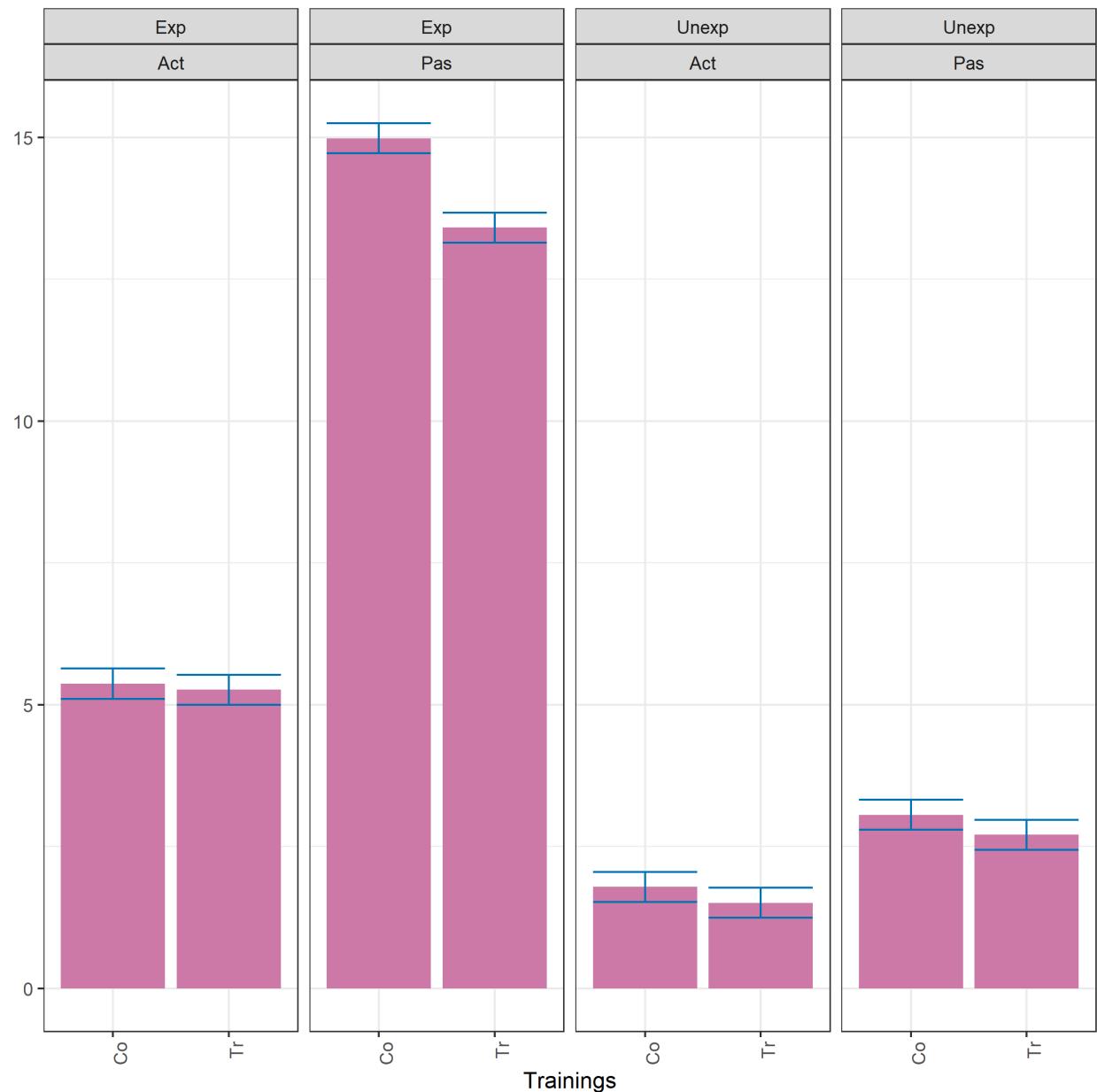


Figure 3: plot of chunk unnamed-chunk-11

**Initial allocation model,
equal variances**

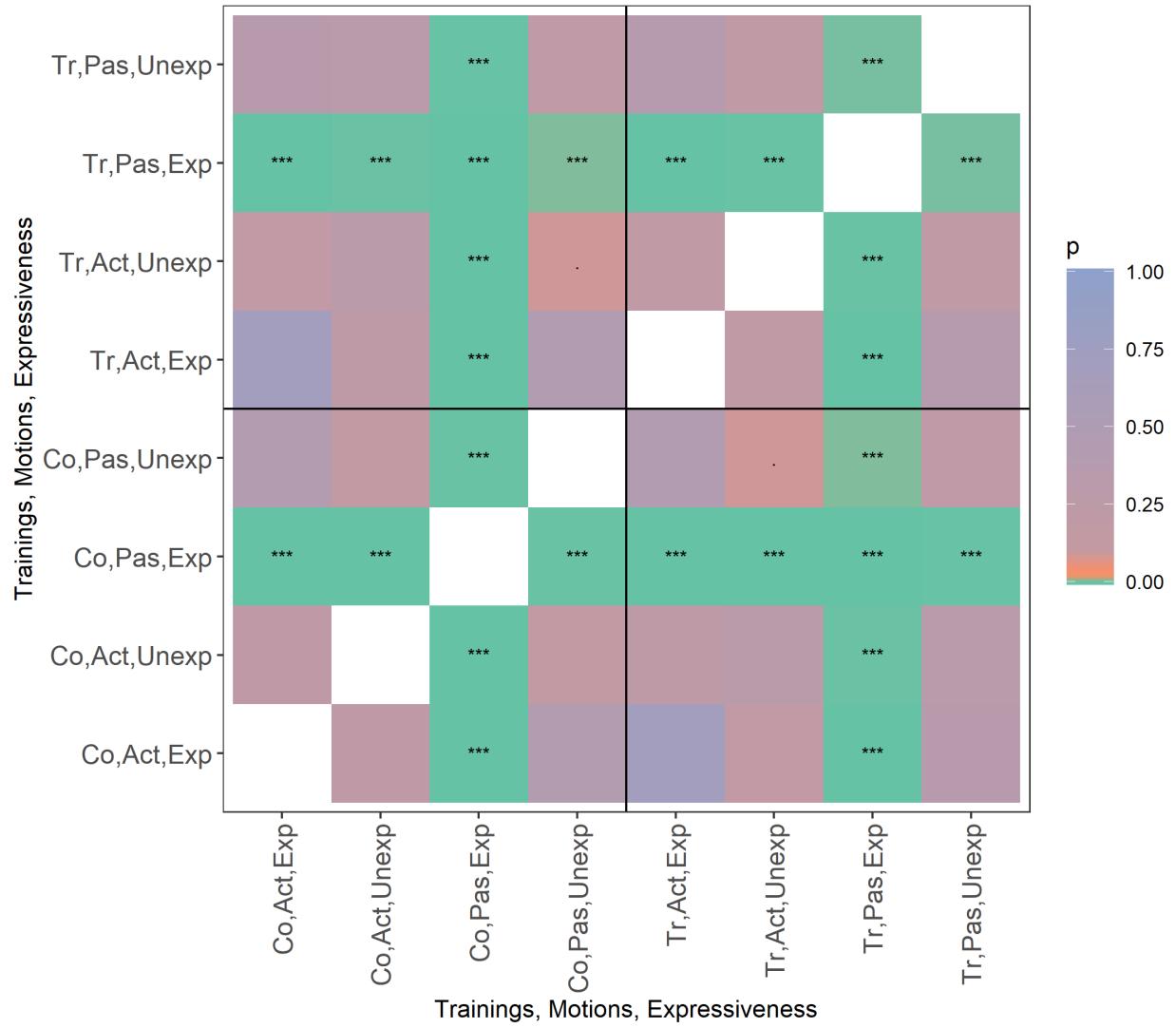


Figure 4: plot of chunk unnamed-chunk-11

Fit model b) no intertier variances and unequal residual variances to see whether heterogeneous variances improves on model a)

```

mb.asrt <- changeModelOnIC(ma.asrt,
                           newResidual = "idh(MotionsExpress):WMotionsExpress",
                           label = "Try heterogeneous variances",
                           IClikelihood = "REML", which.IC = "AIC")

## Calculating denominator DF
## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.liik, bound.exclusions = bound.exclusions:
##   MotionsExpress:WMotionsExpress!R
## Calculating denominator DF
## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.liik, : The following b
##   MotionsExpress:WMotionsExpress!R
(mb.asrt)

##
##
## ##### Summary of the fitting of the variance parameters
##
##                                         component std.error z.ratio bound %ch
## Viewings                               1.42818170 0.86894323 1.6435846 P  0
## Expressiveness:Patients                14.56566580 8.85614901 1.6446952 P  0
## Raters                                 0.01013582 0.01764610 0.5743944 P  0
## MotionsExpress:WMotionsExpress!R      1.00000000 NA             NA       F  0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Exp 1.22114639 0.10279027 11.8799803 P  0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Unexp 0.70625810 0.06064689 11.6454126 P  0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Exp   13.77992460 1.14420141 12.0432684 P  0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Unexp 2.43812281 0.20364308 11.9725294 P  0
##
##
## ##### Pseudo-anova table for fixed terms
##
## Wald tests for fixed effects.
## Response: Y
##
##                                         Df denDF  F.inc     Pr
## (Intercept)                      1    6.0 18.070 0.0054
## Trainings                         1   71.9 13.650 0.0004
## Motions                            1    5.9 65.700 0.0002
## Expressiveness                     1    6.0  7.088 0.0374
## Trainings:Motions                 1 544.6  2.958 0.0860
## Trainings:Expressiveness          1 624.1  0.027 0.8695
## Motions:Expressiveness            1    5.9 39.270 0.0008
## Trainings:Motions:Expressiveness 1 481.0  7.956 0.0050
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##

```

```

##                                     terms DF denDF p      AIC      BIC action
## 1 No intertier variance and equal residual variances 0      4 NA 3041.3081 3061.5876 Starting model
## 2 Try heterogeneous variances   0      3 NA -749.5992 -734.3896     Swapped
AIC.tab <- rbind(AIC.tab, infoCriteria(mb.asrt$asreml.obj))

## Warning in infoCriteria(asreml(mb.asrt$asreml.obj)): The following bound terms were discounted:
## MotionsExpress:WMotionsExpress!R

Extract standardized residuals and fitted values and produce diagnostic plots

plotDiagnostics(mb.asrt, plaid.dat)

```

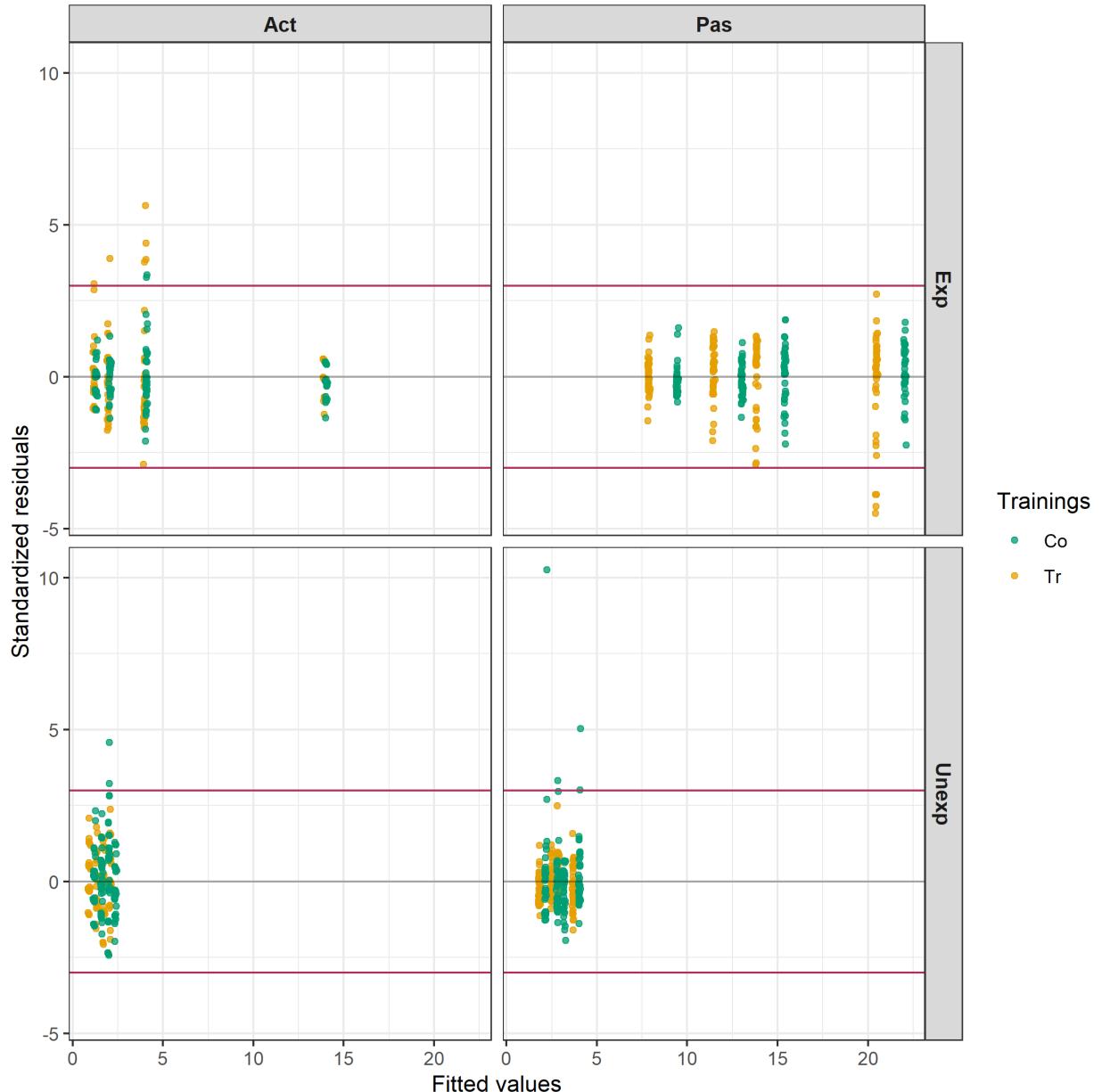


Figure 5: plot of chunk asr_mb

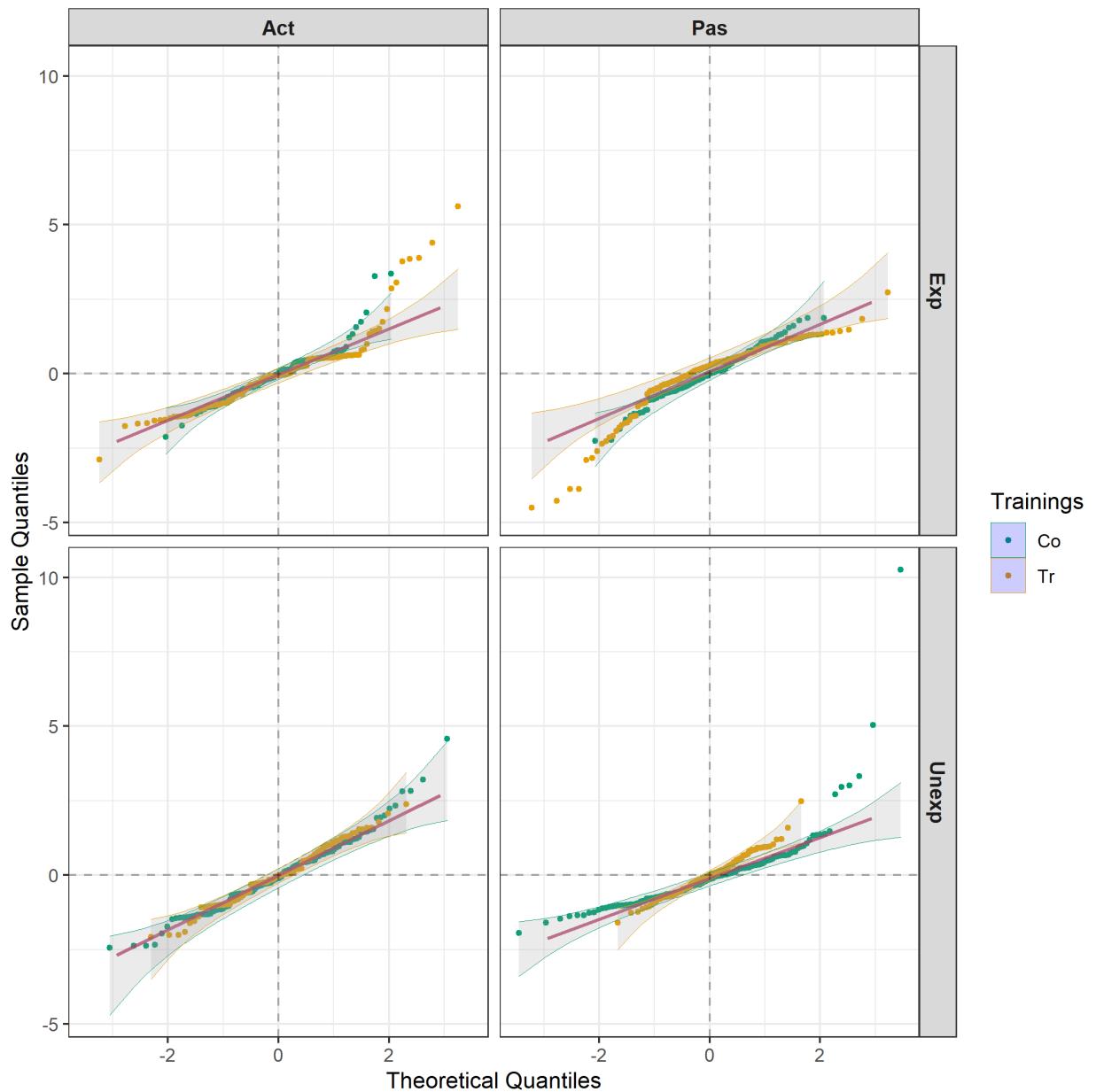


Figure 6: plot of chunk asr_mb

Get and plot predictions

```
mb.choice <- chooseModel(mb.asrt, terms.marginality = marg.fix,
                           denDF="numeric")

## Calculating denominator DF

chosen.terms <- unlist(mb.choice$sig.terms)
submod <- length(chosen.terms) != 1 && chosen.terms != "Trainings:Motions:Expressiveness"
mb.asr <- mb.asrt$asreml.obj
mb.diffs <- predictPlus(mb.asr, classify = "Trainings:Motions:Expressiveness",
                        error.intervals = "half", meanLSD.type = "factor",
                        LSDby = c("Motions", "Expressiveness"), Vmatrix = TRUE,
                        wald = mb.asrt$wald.tab, tables = "none")
```

If the chosen fixed model is a submodel of T:M:E, transform predictions to conform to the chosen model

```
if (submod)
{
  mb.TMEDiffs <- mb.diffs #save full diffs
  submod.ch <- paste("~", paste(chosen.terms, collapse = " + "))
  cat("\n\n#### Chosen model: ", submod.ch, "\n\n")
  mb.diffs <- linTransform(mb.diffs,
                           linear.transformation = as.formula(submod.ch),
                           classify = "Trainings:Motions:Expressiveness",
                           error.intervals = "half", meanLSD.type = "factor",
                           LSDby = c("Motions", "Expressiveness"),
                           wald = mb.asrt$wald.tab, tables = "none")
}
else
  cat("\n\n#### Chosen model: ~ Trainings:Motions:Expressiveness\n\n")

##
##
## #### Chosen model: ~ Trainings:Motions:Expressiveness
(mb.diffs$predictions)

##
##
## #### Predictions
##
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
##   calculated from model terms constructed solely from factors in
##   the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - The ignored set: Raters,Viewings,Patients
##
##
##   Trainings Motions Expressiveness predicted.value standard.error upper.halfLeastSignificant.limit
## 1      Co     Act          Exp      5.370101      2.001746      5.498385
## 2      Co     Act        Unexp      1.790563      2.000877      1.889259
## 3      Co     Pas          Exp     14.982800      2.022830      15.407378
```

```

## 4      Co    Pas        Unexp     3.057149     2.003799     3.236955
## 5      Tr    Act        Exp      5.261824     2.001746     5.390108
## 6      Tr    Act        Unexp    1.508846     2.000877     1.607542
## 7      Tr    Pas        Exp      13.407878    2.022830    13.832457
## 8      Tr    Pas        Unexp    2.705541     2.003799     2.885347
##   lower.halfLeastSignificant.limit est.status
## 1                          5.241817 Estimable
## 2                          1.691867 Estimable
## 3                         14.558221 Estimable
## 4                         2.877342 Estimable
## 5                         5.133540 Estimable
## 6                         1.410150 Estimable
## 7                        12.983300 Estimable
## 8                        2.525734 Estimable

plotPredictions(mb.diffs$predictions, classify = "Trainings:Motions:Expressiveness",
                y = "predicted.value",
                error.intervals = "half", interval.annotate = FALSE,
                ggpplotFuncs = list(facet_grid(cols = vars(Expressiveness, Motions)))))

plotPvalues(mb.diffs, factors.per.grid = 2, show.sig = TRUE,
            title = "Initial allocation model, \nunequal variances")

```

Fit the full prior allocation model, except for identity terms, to show that it is nonsingular

```

mfull.asr <- asreml(Y ~ Trainings * Motions * Expressiveness,
                      random = ~ Raters + Viewings +
                                Expressiveness:Patients/(Occasions + Trainings*Motions) +
                                Raters:(Motions*Expressiveness) + Raters:Expressiveness:Patients,
                      aom = TRUE, data = plaid.dat)

## Model fitted using the gamma parameterization.
## ASReml 4.1.0 Mon Mar 22 16:42:34 2021
##          LogLik      Sigma2      DF      wall      cpu
## 1      -1521.361    3.35511    1176 16:42:34      0.0 (1 restrained)
## 2 singularities in the Average Information matrix.

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 2      -1503.359    3.41238    1176 16:42:34      0.0 (2 restrained)

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 3      -1487.165    3.42477    1176 16:42:34      0.0 (2 restrained)

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 4      -1479.065    3.34427    1176 16:42:34      0.0 (2 restrained)

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 5      -1474.862    3.29448    1176 16:42:34      0.0 (2 restrained)

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in

```

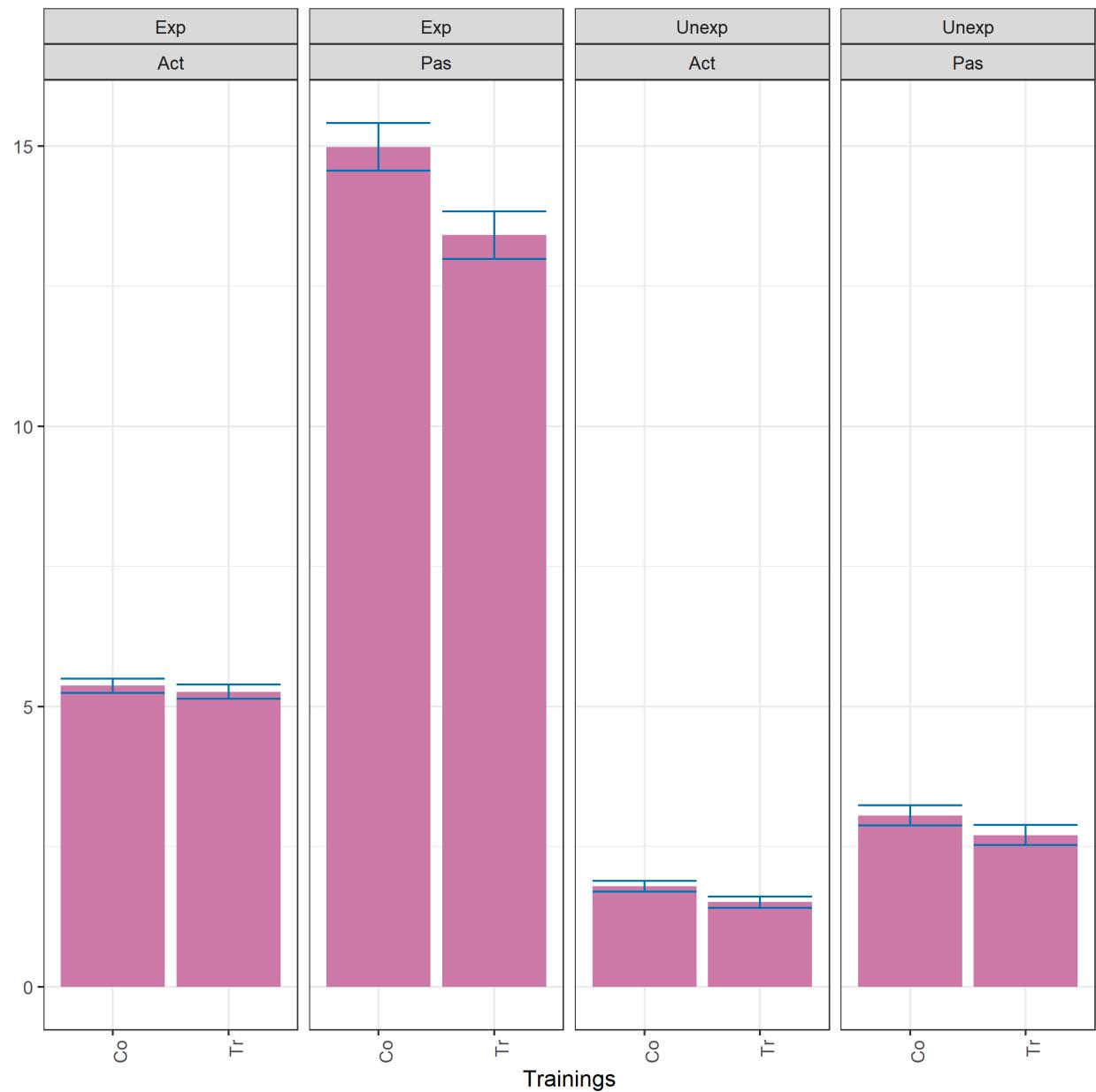


Figure 7: plot of chunk unnamed-chunk-13

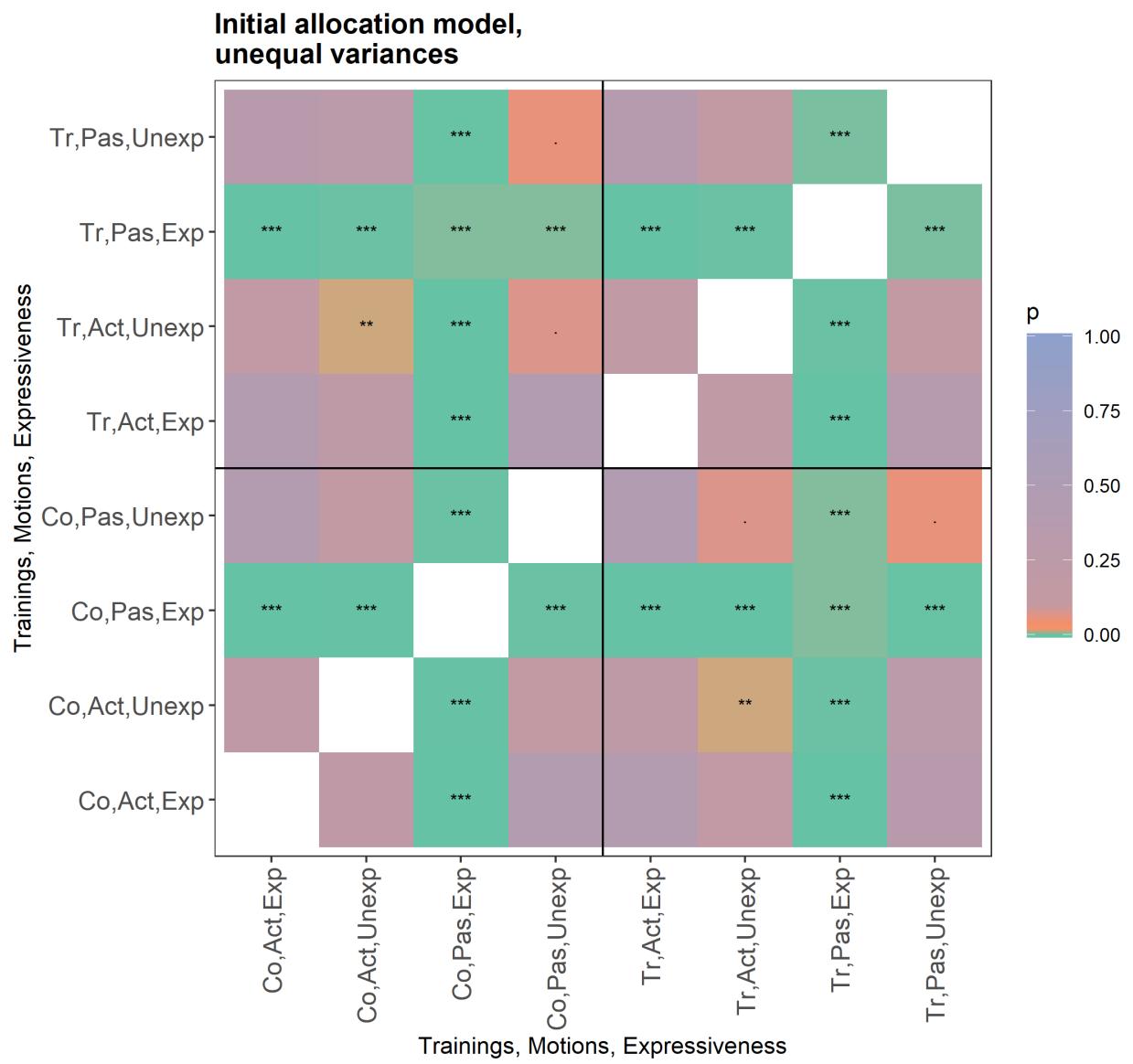


Figure 8: plot of chunk unnamed-chunk-13

```

## the average information matrix.

## 6      -1473.456      3.27809    1176 16:42:34      0.0 (1 restrained)

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 7      -1473.139      3.27117    1176 16:42:34      0.0

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 8      -1473.109      3.26898    1176 16:42:34      0.0

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 9      -1473.109      3.26870    1176 16:42:34      0.0

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

## 10     -1473.109      3.26870    1176 16:42:35      0.2

## Warning in asreml(Y ~ Trainings * Motions * Expressiveness, random = ~Raters + : Singularities in
## the average information matrix.

summary(mfull.asr)$varcomp
```

	component	std.error	z.ratio	bound	%ch
## Viewings	7.609710e-01	0.89785598	0.847542398	P	0
## Expressiveness:Patients	1.448199e+01	8.81982538	1.641981274	P	0
## Expressiveness:Patients:Occasions	3.268700e-01	0.01572654	20.784609706	S	0
## Expressiveness:Patients:Trainings	5.324598e-04	0.10938702	0.004867669	P	0
## Expressiveness:Patients:Motions	3.268700e-01	0.01572654	20.784609706	S	0
## Expressiveness:Patients:Trainings:Motions	1.790661e-01	0.15444738	1.159399042	P	0
## Raters	1.280818e-06	NA	NA	B	0
## Raters:Motions	8.099187e-02	0.17004892	0.476285690	P	0
## Raters:Expressiveness	7.684186e-02	0.16999557	0.452022694	P	0
## Raters:Motions:Expressiveness	1.068292e+00	0.28250325	3.781522160	P	0
## Raters:Expressiveness:Patients	1.665475e-07	NA	NA	B	NA
## units!R	3.268700e+00	0.15726541	20.784609706	P	0

Change to model c), the nonsingular prior allocation model with intertier variances and equal residual variances

Drop singular terms OPE and MPE, identified using the EMS (and confirmed by asreml)

```

mc.asr <- asreml(Y ~ Trainings * Motions * Expressiveness,
                    random = ~Raters+Viewings+
                           Expressiveness:Patients/Trainings/Motions+
                           Raters:(Occurrences*Expressiveness) + Raters:Expressiveness:Patients,
                    aom = TRUE, data = plaid.dat)

## Model fitted using the gamma parameterization.
## ASReml 4.1.0 Mon Mar 22 16:42:35 2021
##          LogLik      Sigma2      DF      wall      cpu
## 1      -1539.710      3.48193    1176 16:42:35      0.0 (1 restrained)
## 2      -1518.288      3.52565    1176 16:42:35      0.0 (2 restrained)
## 3      -1495.651      3.48752    1176 16:42:35      0.0 (2 restrained)
```

```

## 4 -1483.282 3.37667 1176 16:42:35 0.0 (2 restrained)
## 5 -1476.498 3.30912 1176 16:42:35 0.0 (2 restrained)
## 6 -1473.964 3.28475 1176 16:42:35 0.0 (1 restrained)
## 7 -1473.231 3.27393 1176 16:42:35 0.0
## 8 -1473.114 3.26970 1176 16:42:35 0.0
## 9 -1473.109 3.26875 1176 16:42:35 0.0
## 10 -1473.109 3.26870 1176 16:42:35 0.1

summary(mc.asr)$varcomp

##                                     component std.error    z.ratio bound %ch
## Viewings                         1.414711e+00 0.8973050 1.57662240 P  0
## Expressiveness:Patients           1.448199e+01 8.8196925 1.64200609 P  0
## Expressiveness:Patients:Trainings 5.324600e-04 0.1093870 0.00486767 P  0
## Expressiveness:Patients:Trainings:Motions 1.790662e-01 0.1544474 1.15939901 P  0
## Raters                           1.131598e-06      NA          NA     NA B  0
## Raters:Occasions                 8.099201e-02 0.1700489 0.47628649 P  0
## Raters:Expressiveness            7.684200e-02 0.1699956 0.45202350 P  0
## Raters:Occasions:Expressiveness 1.068292e+00 0.2825032 3.78152187 P  0
## Raters:Expressiveness:Patients   1.603566e-07      NA          NA     NA B  NA
## units!R                          3.268700e+00 0.1572654 20.78460917 P  0

printFormulae(mc.asr)

## 
## 
## ##### Formulae from asreml object
## 
## fixed: Y ~ Trainings * Motions * Expressiveness
## random: ~ Raters + Viewings + Expressiveness:Patients/Trainings/Motions + Raters:(Occasions * Expressiveness)
## residual: NULL

```

Allow negative variance components so equivalent to ANOVA

```

terms <- names(mc.asr$vparameters)
terms <- terms[-length(terms)]
mc.neg.asr <- setvarianceterms(mc.asr$call, terms = terms, bounds = "U")

```

```

## Model fitted using the gamma parameterization.
## ASReml 4.1.0 Mon Mar 22 16:42:35 2021
##          LogLik      Sigma2      DF      wall      cpu
## 1 -1539.710 3.48193 1176 16:42:35 0.0 (1 restrained)
## 2 -1518.288 3.52565 1176 16:42:35 0.0 (2 restrained)
## 3 -1495.651 3.48752 1176 16:42:35 0.0 (2 restrained)
## 4 -1483.282 3.37667 1176 16:42:35 0.0 (2 restrained)
## 5 -1476.495 3.30977 1176 16:42:35 0.0 (2 restrained)
## 6 -1473.939 3.29094 1176 16:42:35 0.0 (2 restrained)
## 7 -1473.104 3.32005 1176 16:42:35 0.0
## 8 -1472.959 3.35597 1176 16:42:35 0.0
## 9 -1472.954 3.35462 1176 16:42:35 0.0
## 10 -1472.954 3.35457 1176 16:42:35 0.1

```

Prepare to use asremlPlus

```

mc.neg.asrt <- as.asrtests(mc.neg.asr, NULL, NULL, IClikelikelihood = "REML",
                           label = "Intertier interactions and unconstrained components")

## Calculating denominator DF
(mc.neg.asrt)

##
##
## ##### Summary of the fitting of the variance parameters
##
##                               component std.error      z.ratio bound %ch
## Viewings                      1.414711088 0.8973049  1.57662241    U  0
## Expressiveness:Patients        14.481988677 8.8197254  1.64199994    U  0
## Expressiveness:Patients:Trainings 0.002853368 0.1094696  0.02606538    U  0
## Expressiveness:Patients:Trainings:Motions 0.176745246 0.1545121  1.14389266    U  0
## Raters                         -0.018172606 0.1705225 -0.10657012    U  0
## Raters:Occasions               0.097802882 0.2321986  0.42120354    U  0
## Raters:Expressiveness          0.115047665 0.2349919  0.48958140    U  0
## Raters:Occasions:Expressiveness 1.031395356 0.3168537  3.25511533    U  0
## Raters:Expressiveness:Patients -0.085873419 0.1573197 -0.54585297    U  0
## units!R                        3.354573808 0.2282498 14.69693817    P  0
##
##
## ##### Pseudo-anova table for fixed terms
##
## Wald tests for fixed effects.
## Response: Y
##
##                               Df denDF   F.inc     Pr
## (Intercept)                 1   6.0 18.900 0.0048
## Trainings                   1  13.7  6.417 0.0242
## Motions                      1   6.5 63.310 0.0001
## Trainings:Motions            1  12.7  2.951 0.1101
## Expressiveness                1   6.0  7.338 0.0352
## Trainings:Expressiveness     1  12.9  1.361 0.2645
## Motions:Expressiveness       1   6.4 36.460 0.0007
## Trainings:Motions:Expressiveness 1  11.5  2.574 0.1357
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##                               terms DF denDF   p      AIC      BIC      action
## 1 Intertier interactions and unconstrained components  0     10 NA 2965.908 3016.607 Starting model
printFormulae(mc.neg.asr)

##
##
## ##### Formulae from asreml object
##
## fixed: Y ~ Trainings * Motions * Expressiveness

```

```

## random: ~ Raters + Viewings + Expressiveness:Patients/Trainings/Motions + Raters:(Occurrences * Expressiveness)
## residual: NULL
AIC.tab <- rbind(AIC.tab, infoCriteria(mc.neg.asrt$asreml.obj))

```

Extract standardized residuals and fitted values and produce diagnostic plots

```
plotDiagnostics(mc.neg.asrt, plaid.dat)
```

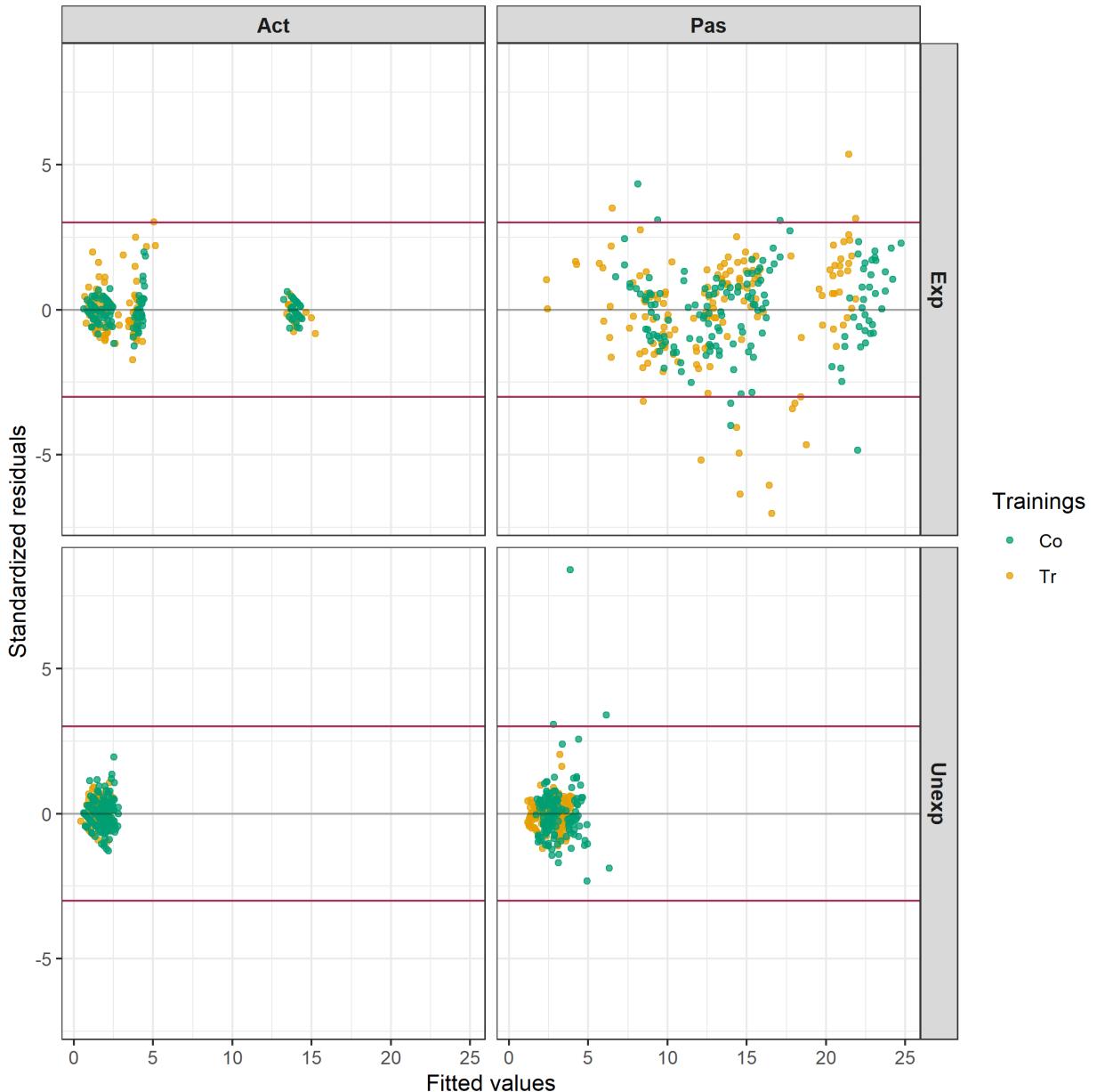


Figure 9: plot of chunk asr_mc

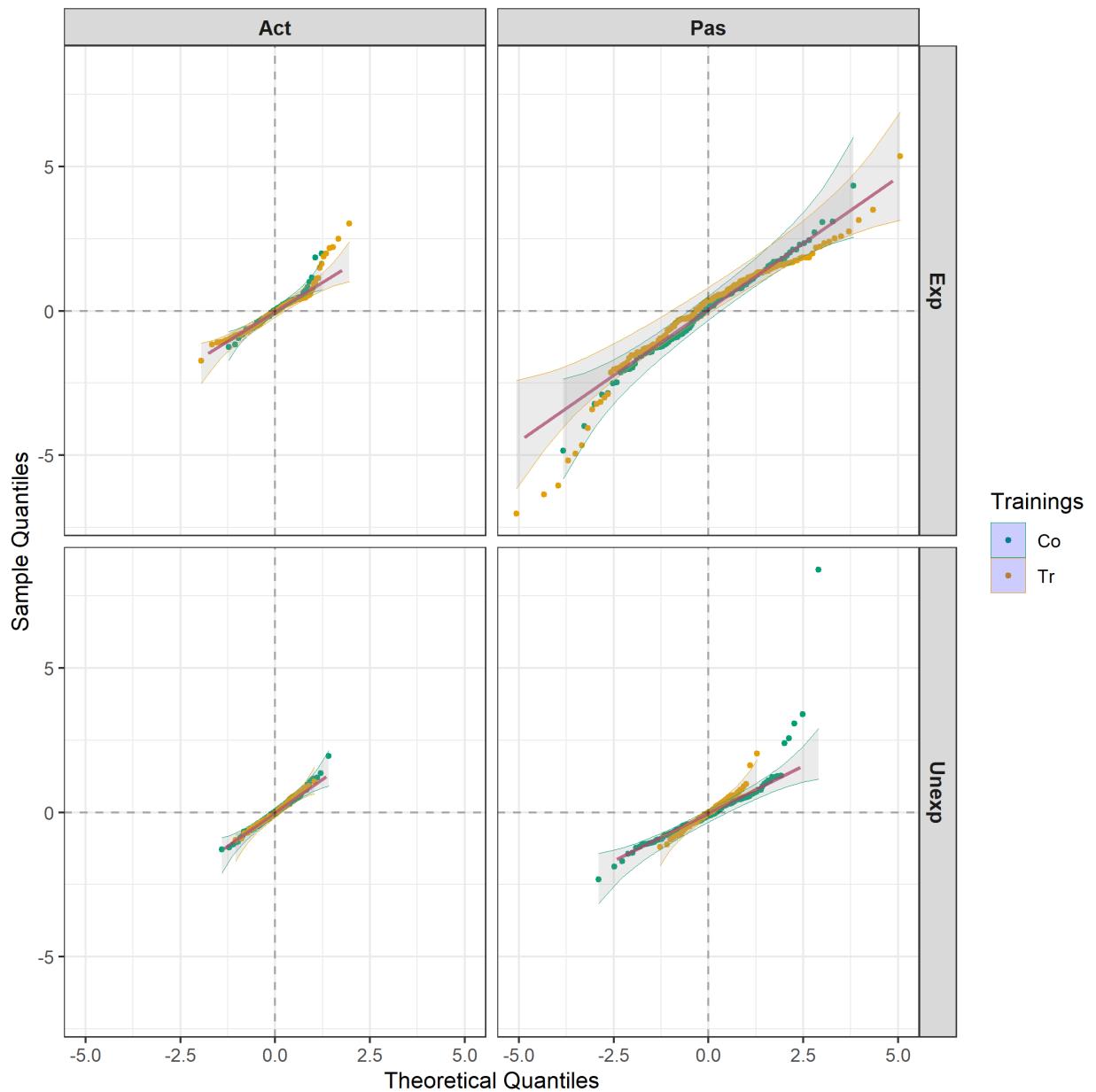


Figure 10: plot of chunk asr_mc

Get and plot predictions based on the nonsingular models with intertier interactions

```
mc.neg.choice <- chooseModel(mc.neg.asrt, terms.marginality = marg.fix,
                               denDF="numeric")

## Calculating denominator DF

chosen.terms <- unlist(mc.neg.choice$sig.terms)
submod <- length(chosen.terms) != 1 && chosen.terms != "Trainings:Motions:Expressiveness"
mc.neg.diffs <- predictPlus(mc.neg.asr, classify = "Trainings:Motions:Expressiveness",
                             error.intervals = "half", meanLSD.type = "factor",
                             LSDby = c("Motions", "Expressiveness"), Vmatrix = TRUE,
                             wald = mc.neg.asrt$wald.tab, tables = "none")
```

If the chosen fixed model is a submodel of T:M:E, transform predictions to conform to the chosen model

```
if (submod)
{
  mc.neg.TMEDiffs <- mc.neg.diffs #save full diffs
  submod.ch <- paste("~", paste(chosen.terms, collapse = " + "))
  cat("\n\n#### Chosen model: ", submod.ch, "\n\n")
  mc.neg.diffs <- linTransform(mc.neg.diffs,
                                linear.transformation = as.formula(submod.ch),
                                classify = "Trainings:Motions:Expressiveness",
                                error.intervals = "half", meanLSD.type = "factor",
                                LSDby = c("Motions", "Expressiveness"),
                                wald = mc.neg.asrt$wald.tab, tables = "none")
}
else
  cat("\n\n#### Chosen model: ~ Trainings:Motions:Expressiveness\n\n")

##
##
## #### Chosen model: ~ Motions:Expressiveness + Trainings
(mc.neg.diffs$predictions)

##
##
## #### Predictions
##
##
## Notes:
## The original predictions, obtained as described below, have
## been linearly transformed to form estimated marginal means.
## - The predictions are obtained by averaging across the hypertable
##   calculated from model terms constructed solely from factors in
##   the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - The ignored set: Raters,Viewings,Patients,Occasions
##
```

```

## 
##   Trainings Motions Expressiveness predicted.value standard.error upper.halfLeastSignificant.limit
## 1       Co     Act          Exp      5.605528    2.009304           5.8555796
## 2       Co     Act        Unexp     1.939270    2.009304           2.189537
## 3       Co     Pas          Exp     14.484904    2.009304          14.735172
## 4       Co     Pas        Unexp     3.170910    2.009304           3.421177
## 5       Tr     Act          Exp      5.026397    2.009304           5.276665
## 6       Tr     Act        Unexp     1.360139    2.009304           1.610406
## 7       Tr     Pas          Exp     13.905774    2.009304          14.156041
## 8       Tr     Pas        Unexp     2.591779    2.009304           2.842046
##   lower.halfLeastSignificant.limit est.status
## 1                   5.355261 Estimable
## 2                   1.689003 Estimable
## 3                  14.234637 Estimable
## 4                  2.920643 Estimable
## 5                  4.776130 Estimable
## 6                  1.109872 Estimable
## 7                 13.655506 Estimable
## 8                 2.341512 Estimable

plotPredictions(mc.neg.diffs$predictions, classify = "Trainings:Motions:Expressiveness",
                y = "predicted.value",
                error.intervals = "half", interval.annotate = FALSE,
                ggplotFuncs = list(facet_grid(cols = vars(Expressiveness, Motions)))))

plotPvalues(mc.neg.diffs, factors.per.grid = 2, show.sig = TRUE,
            title = "Prior allocation model, \nunequal variances")

```

Fit model d) with intertier variances and unequal residual variances

```

md.asr <- asreml(Y ~ Trainings * Motions * Expressiveness,
                    random = ~ Raters+ Viewings +
                      Expressiveness:Patients/Trainings/Motions +
                      Raters:(Occurrences*Expressiveness) + Raters:Expressiveness:Patients,
                    residual = ~ idh(MotionsExpress):WMotionsExpress,
                    maxit = 50, aom = TRUE,
                    data = plaid.dat)

## Model fitted using the sigma parameterization.
## ASReml 4.1.0 Mon Mar 22 16:42:46 2021
## 
##   LogLik      Sigma2     DF    wall    cpu
## 1 -1659.584     1.0 1176 16:42:47 0.0 (8 restrained)
## 2 -1194.037     1.0 1176 16:42:47 0.0 (4 restrained)
## 3 -1141.100     1.0 1176 16:42:47 0.0 (1 restrained)
## 4 -1134.016     1.0 1176 16:42:47 0.0 (3 restrained)
## 5 -1132.870     1.0 1176 16:42:47 0.0 (2 restrained)
## 6 -1132.700     1.0 1176 16:42:47 0.0 (4 restrained)
## 7 -1133.077     1.0 1176 16:42:47 0.0 (3 restrained)
## 8 -1132.688     1.0 1176 16:42:47 0.0 (2 restrained)
## 9 -1132.622     1.0 1176 16:42:47 0.0 (3 restrained)
## 10 -1133.282    1.0 1176 16:42:47 0.0 (2 restrained)
## 11 -1132.750    1.0 1176 16:42:47 0.0
## 12 -1132.629    1.0 1176 16:42:47 0.0
## 13 -1132.621    1.0 1176 16:42:47 0.0

```

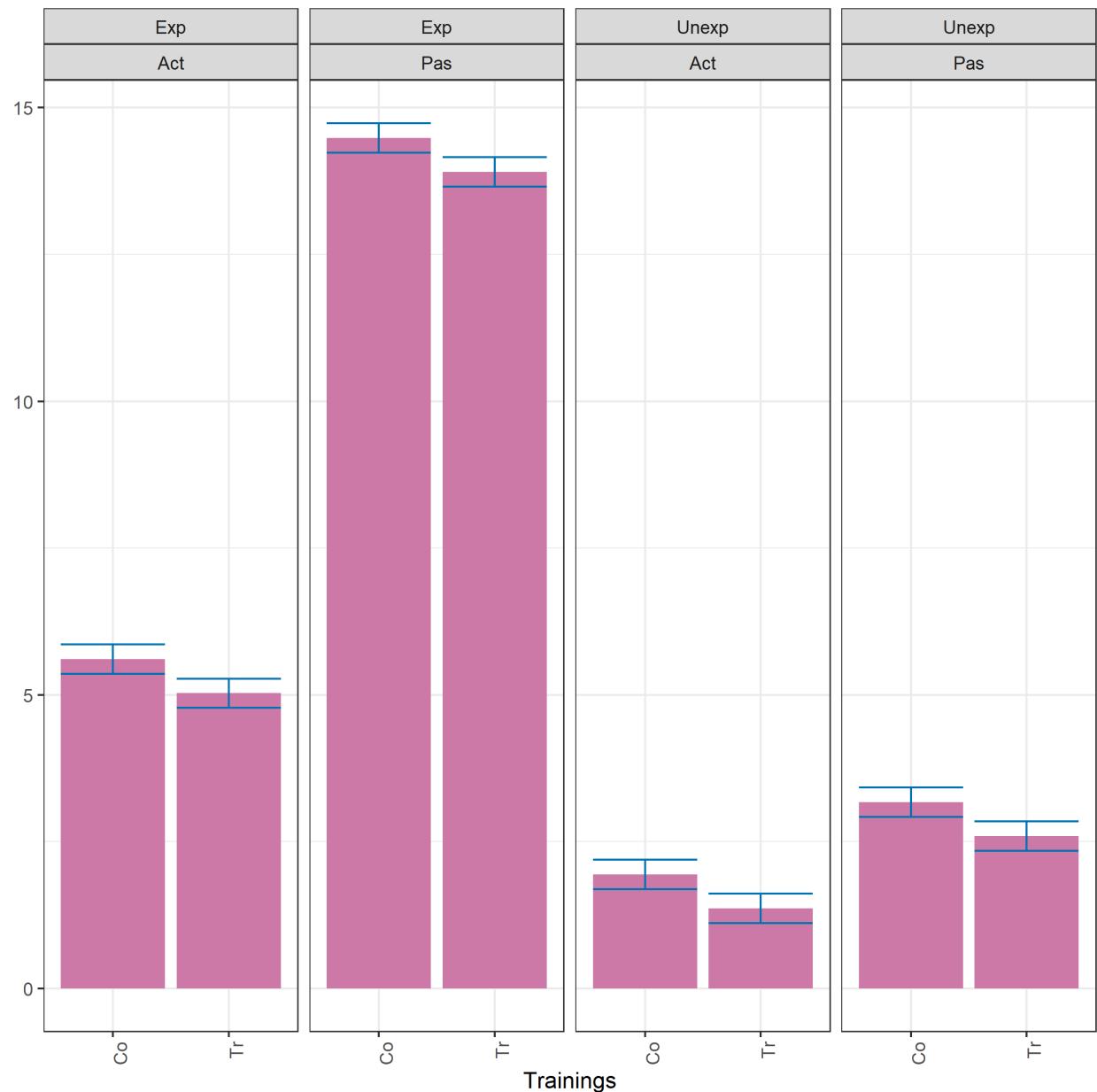


Figure 11: plot of chunk unnamed-chunk-18

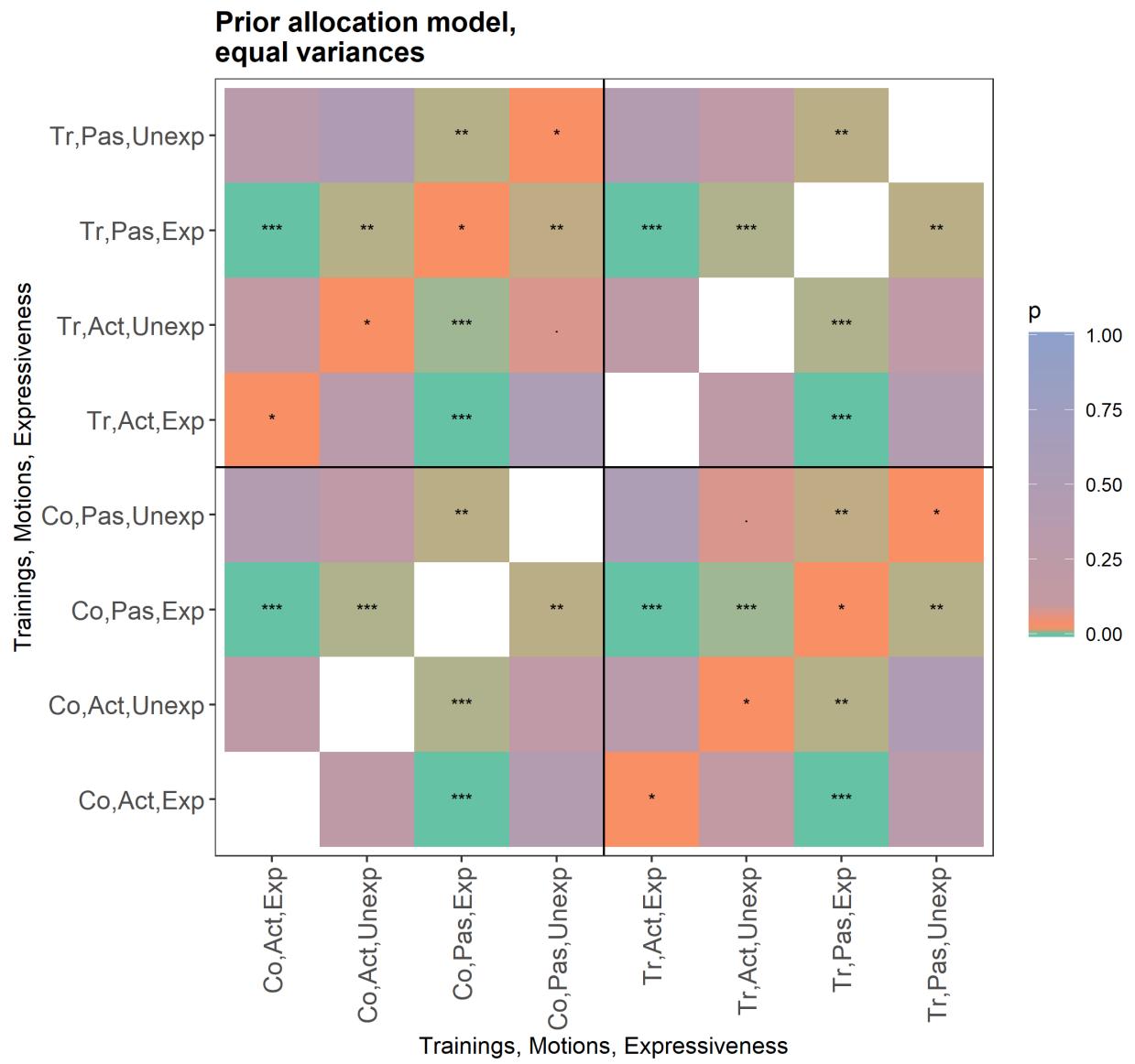


Figure 12: plot of chunk unnamed-chunk-18

```
## 14      -1132.621          1.0    1176 16:42:47     0.1
```

Prepare to use asremlPlus

```
md.asrt <- as.asrtests(md.asr, NULL, NULL, IClikelhood = "REML",
                        label = "Intertier variance and unequal residual variances")

## Warning in infoCriteria.asreml(asreml.obj, IClikelhood = ic.lik, bound.exclusions = bound.exclusions:
##   Raters:Occasions, Raters:Expressiveness, Raters:Occasions:Expressiveness, MotionsExpress:WMotionsExp

## Calculating denominator DF
(md.asrt)

##
##
## ##### Summary of the fitting of the variance parameters
##
##                                         component std.error z.ratio bound
## Viewings                                1.400908e+00 0.86897501 1.6121380 P
## Expressiveness:Patients                  1.456116e+01 8.85623965 1.6441697 P
## Expressiveness:Patients:Trainings       5.040427e-03 0.04463139 0.1129346 P
## Expressiveness:Patients:Trainings:Motions 5.717214e-02 0.06081453 0.9401066 P
## Raters                                    1.840418e-03 0.01793428 0.1026201 P
## Raters:Occasions                         1.304646e-07 NA             NA        B
## Raters:Expressiveness                   1.304646e-07 NA             NA        B
## Raters:Occasions:Expressiveness         1.304646e-07 NA             NA        B
## Raters:Expressiveness:Patients          1.862729e-01 0.07477739 2.4910326 P
## MotionsExpress:WMotionsExpress!R        1.000000e+00 NA             NA        F
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Exp 1.054088e+00 0.12381945 8.5131048 P
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Unexp 5.034771e-01 0.08401565 5.9926589 P
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Exp  1.368750e+01 1.15101141 11.8917194 P
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Unexp 2.176451e+00 0.19672484 11.0634281 P
##                                         %ch
## Viewings                                0.0
## Expressiveness:Patients                  0.0
## Expressiveness:Patients:Trainings       0.0
## Expressiveness:Patients:Trainings:Motions 0.0
## Raters                                    0.1
## Raters:Occasions                         0.0
## Raters:Expressiveness                   0.0
## Raters:Occasions:Expressiveness         0.0
## Raters:Expressiveness:Patients          0.0
## MotionsExpress:WMotionsExpress!R        0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Exp 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Unexp 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Exp  0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Unexp 0.0
##
##
## ##### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: Y
```

```

##                                     Df denDF  F.inc     Pr
## (Intercept)                      1   6.0 18.070 0.0054
## Trainings                         1   6.1  6.512 0.0428
## Motions                           1   5.9 65.700 0.0002
## Trainings:Motions                 1   7.3  2.622 0.1477
## Expressiveness                     1   6.0  7.088 0.0374
## Trainings:Expressiveness          1   7.3  0.273 0.6171
## Motions:Expressiveness            1   5.9 39.300 0.0008
## Trainings:Motions:Expressiveness 1  16.4  5.578 0.0309
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##                                     terms DF denDF  p      AIC      BIC      action
## 1 Intertier variance and unequal residual variances 0      10 NA 2285.241 2335.94 Starting model
printFormulae(md.asr)

##
##
## ##### Formulae from asreml object
##
## fixed: Y ~ Trainings * Motions * Expressiveness
## random: ~ Raters + Viewings + Expressiveness:Patients/Trainings/Motions + Raters:(Occasions * Expressiveness)
## residual: ~ idh(MotionsExpress):WMotionsExpress

```

Extract standardized residuals and fitted values and produce diagnostic plots

```
plotDiagnostics(md.asrt, plaid.dat)
```

Remove the bound terms

```

md.asrt <- rmboundary(md.asrt)
print(md.asrt, which = "test")

##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##                                     terms DF denDF  p      AIC      BIC      action
## 1 Intertier variance and unequal residual variances 0      10 NA 2285.241 2335.94 Starting model
## 2                               Raters:Expressiveness 1      NA NA      NA      NA      Boundary
## 3                               Raters:Occurrences 1      NA NA      NA      NA      Boundary
## 4 Raters:Expressiveness:Occurrences 1      NA NA      NA      NA      Boundary

```

Test the remaining components for intertier interactions using AIC

```
intvcomps <- md.asrt$asreml.obj$vparameters[c(3:4,6)]
terms <- names(intvcomps)
```

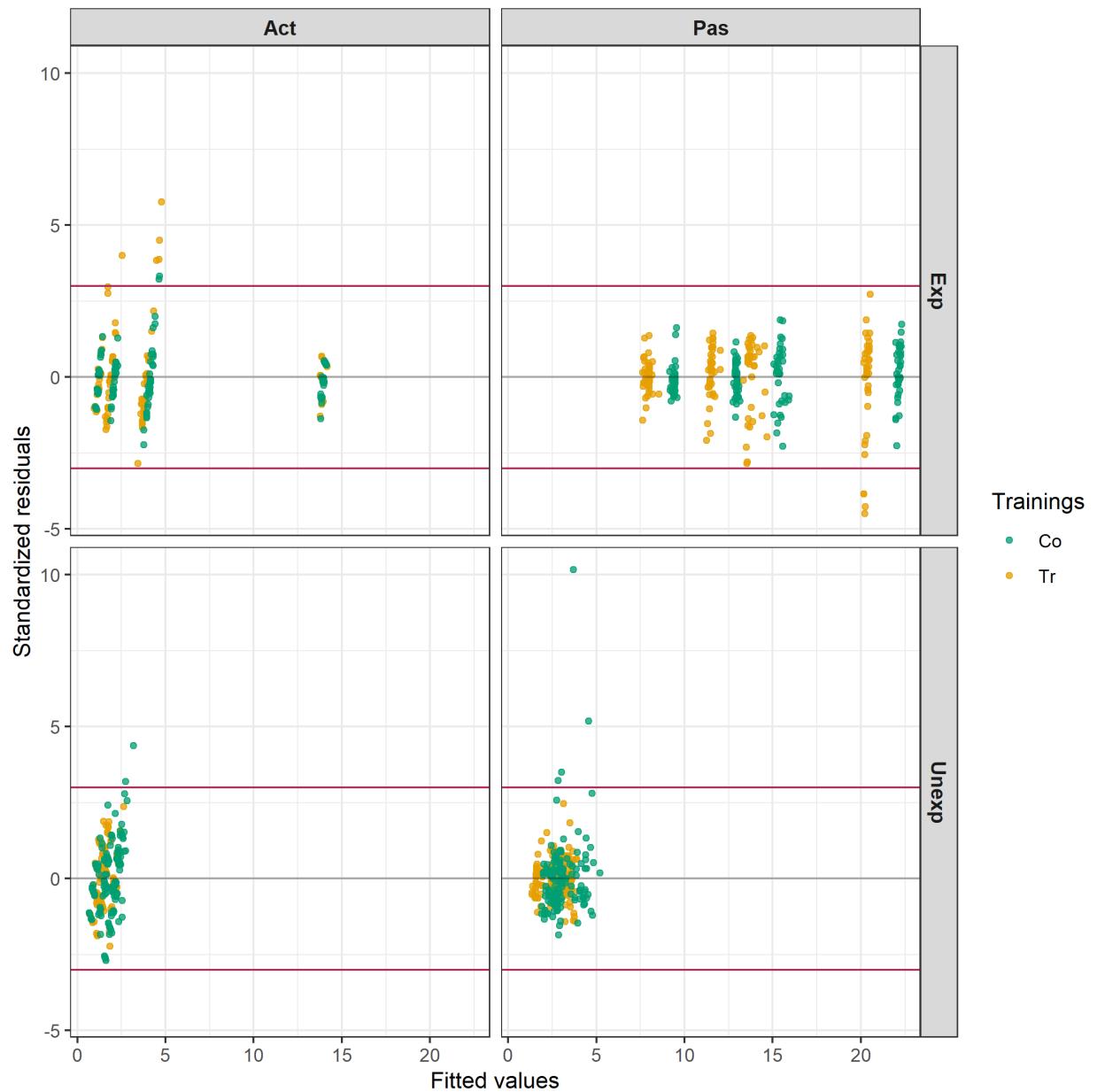


Figure 13: plot of chunk asr_md

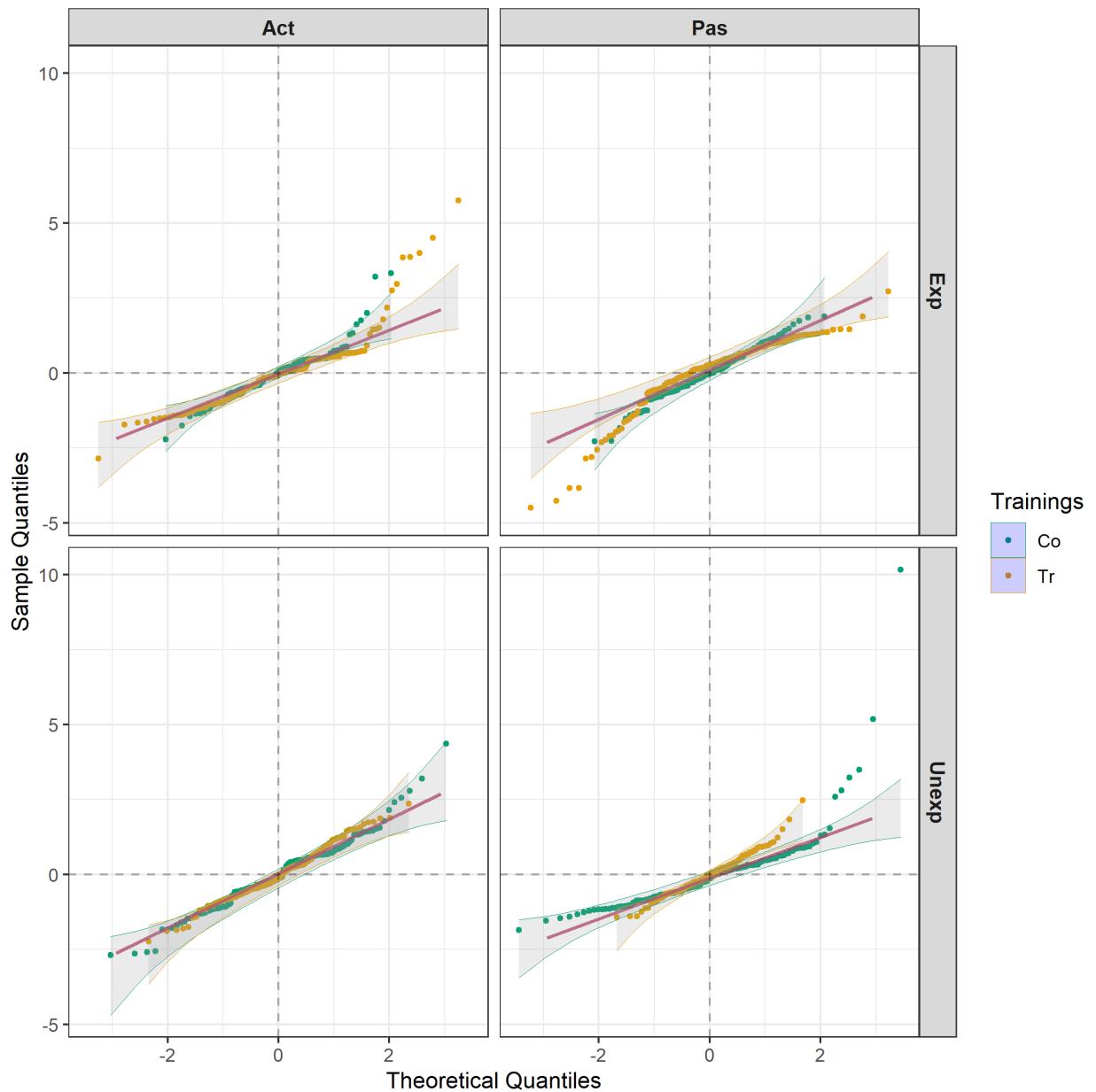


Figure 14: plot of chunk asr_md

```

md.AIC.asrt <- md.asrt
for (term in terms)
  md.AIC.asrt <- changeModelOnIC(md.AIC.asrt, dropRandom = term,
                                    which.IC = "AIC",
                                    label = paste("Try dropping", term))

## Warning in infoCriteria.asreml(asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## Calculating denominator DF

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.li
## MotionsExpress:WMotionsExpress!R

## MotionsExpress:WMotionsExpress!R

(md.AIC.asrt)

##
##
## ###### Summary of the fitting of the variance parameters
##
##                                         component std.error    z.ratio bound
## Viewings                               1.398494383 0.86877041 1.6097399   P
## Expressiveness:Patients                 14.563670533 8.85621923 1.6444569   P
## Expressiveness:Patients:Trainings:Motions 0.062024263 0.04797916 1.2927335   P
## Raters                                 0.001810873 0.01793291 0.1009804   P
## Raters:Expressiveness:Patients          0.186764054 0.07471863 2.4995646   P
## MotionsExpress:WMotionsExpress!R           1.000000000      NA        NA   F
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Exp 1.053617727 0.12377800 8.5121564   P
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Unexp 0.503082797 0.08395296 5.9924365   P
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Exp 13.686303631 1.15093950 11.8914188   P

```

```

## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Unexp 2.176228975 0.19670439 11.0634491 P
##
## Viewings %ch
## Expressiveness:Patients 0.0
## Expressiveness:Patients:Trainings:Motions 0.1
## Raters 0.1
## Raters:Expressiveness:Patients 0.0
## MotionsExpress:WMotionsExpress!R 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Exp 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Act,Unexp 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Exp 0.0
## MotionsExpress:WMotionsExpress!MotionsExpress_Pas,Unexp 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: Y
##
##                               Df denDF   F.inc     Pr
## (Intercept)                 1   6.0 18.070 0.0054
## Trainings                   1   9.2  6.895 0.0271
## Motions                      1   5.9 65.700 0.0002
## Expressiveness                1   6.0  7.088 0.0374
## Trainings:Motions             1  11.9  2.577 0.1346
## Trainings:Expressiveness      1   9.9  0.324 0.5821
## Motions:Expressiveness        1   5.9 39.300 0.0008
## Trainings:Motions:Expressiveness 1  27.5  5.427 0.0274
##
##
## #### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##                               terms DF denDF   p       AIC       BIC
## 1      Intertier variance and unequal residual variances 0    10 NA 2285.241005 2335.9397464
## 2                      Raters:Expressiveness 1    NA NA          NA          NA
## 3                      Raters:Occurrences 1    NA NA          NA          NA
## 4      Raters:Expressiveness:Occurrences 1    NA NA          NA          NA
## 5      Try dropping Expressiveness:Patients:Trainings 0    -1 NA -1.983624 -7.0534978
## 6 Try dropping Expressiveness:Patients:Trainings:Motions 0    -1 NA  3.903492 -1.1663822
## 7      Try dropping Raters:Expressiveness:Patients 0    -1 NA  4.365970 -0.7039041
## action
## 1 Starting model
## 2 Boundary
## 3 Boundary
## 4 Boundary
## 5 Swapped
## 6 Unswapped
## 7 Unswapped
printFormulae(md.AIC.asrt$asreml.obj)

##

```

```

##  

## ##### Formulae from asreml object  

##  

## fixed: Y ~ Trainings + Motions + Expressiveness + Trainings:Motions + Trainings:Expressiveness + Mot...  

## random: ~ Raters + Viewings + Expressiveness:Patients + Raters:Expressiveness:Patients + Expressiven...  

## residual: ~ idh(MotionsExpress):WMotionsExpress  

AIC.tab <- rbind(AIC.tab, infoCriteria(md.AIC.asrt$asreml.obj))

## Warning in infoCriteria.asreml(md.AIC.asrt$asreml.obj): The following bound terms were discounted:  

## MotionsExpress:WMotionsExpress!R

```

Extract standardized residuals and fitted values and produce diagnostic plots

```
plotDiagnostics(md.AIC.asrt, plaid.dat)
```

Get and plot predictions based on models chosen using AIC

```

md.AIC.choice <- chooseModel(md.AIC.asrt, terms.marginality = marg.fix,  

                               denDF="numeric")

## Calculating denominator DF
chosen.terms <- unlist(md.AIC.choice$sig.terms)
submod <- length(chosen.terms) != 1 && chosen.terms != "Trainings:Motions:Expressiveness"
current.asr <- md.AIC.asrt$asreml.obj
md.AIC.diffs <- predictPlus(current.asr, classify = "Trainings:Motions:Expressiveness",
                             error.intervals = "half", meanLSD.type = "factor",
                             LSDby = c("Motions", "Expressiveness"),
                             wald = md.AIC.asrt$wald.tab,
                             Vmatrix = TRUE, tables = "none")

```

If the chosen fixed model is a submodel of T:M:E, transform predictions to conform to the chosen model

```

if (submod)
{
  md.AIC.TMEDiffs <- md.AIC.diffs #save full diffs
  submod.ch <- paste(~, paste(chosen.terms, collapse = " + "))
  cat("\n\n##### Chosen model: ", submod.ch, "\n\n")
  md.AIC.subdiffs <- linTransform(md.AIC.diffs,
                                    linear.transformation = as.formula(submod.ch),
                                    classify = "Trainings:Motions:Expressiveness",
                                    error.intervals = "half", meanLSD.type = "factor",
                                    LSDby = c("Motions", "Expressiveness"),
                                    wald = md.AIC.asrt$wald.tab, tables = "none")
  (md.AIC.subdiffs$predictions)
} else
  cat("\n\n##### Chosen model: ~ Trainings:Motions:Expressiveness\n\n")

##
##
## ##### Chosen model: ~ Trainings:Motions:Expressiveness

```

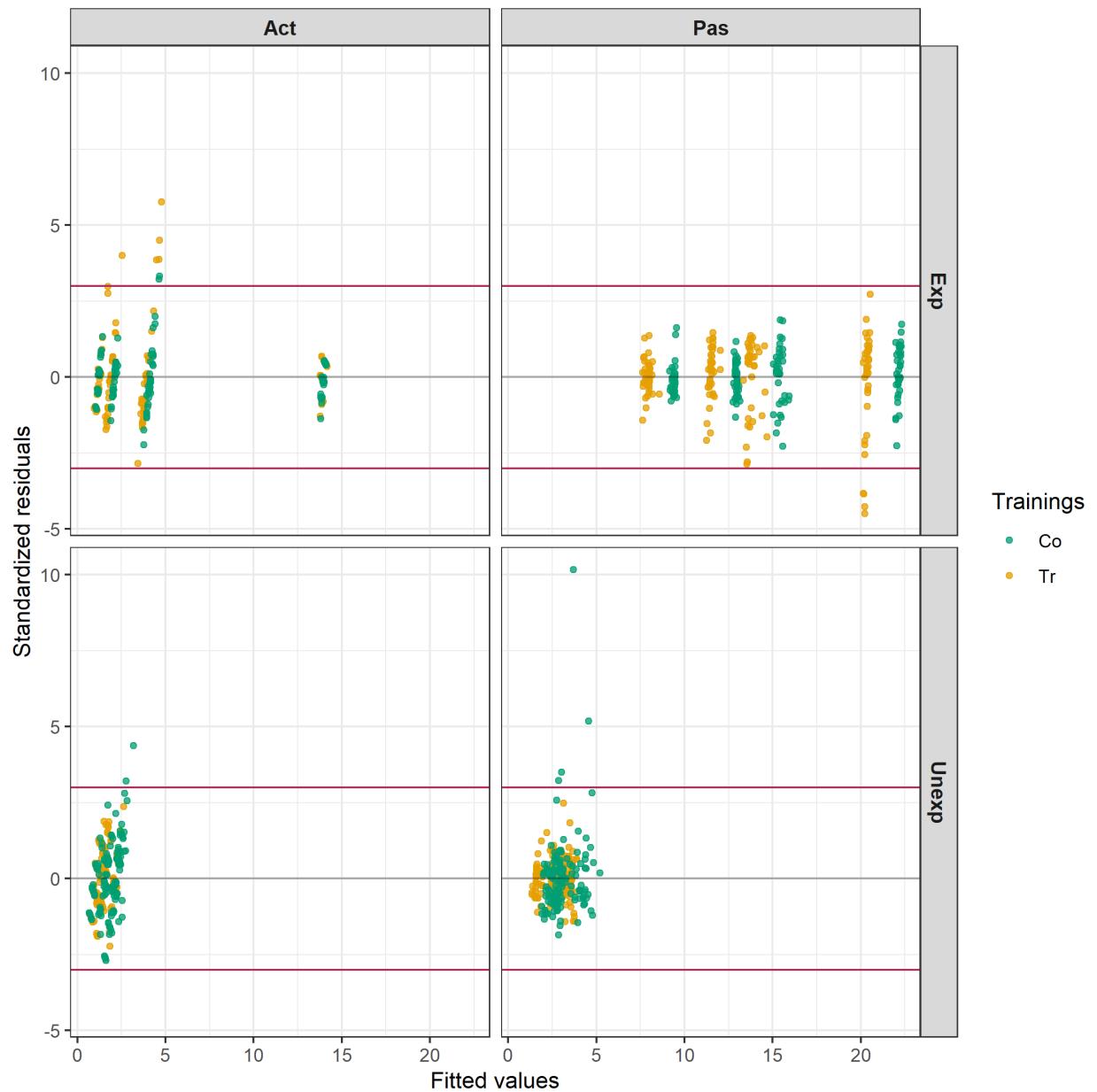


Figure 15: plot of chunk asr_mdAIC

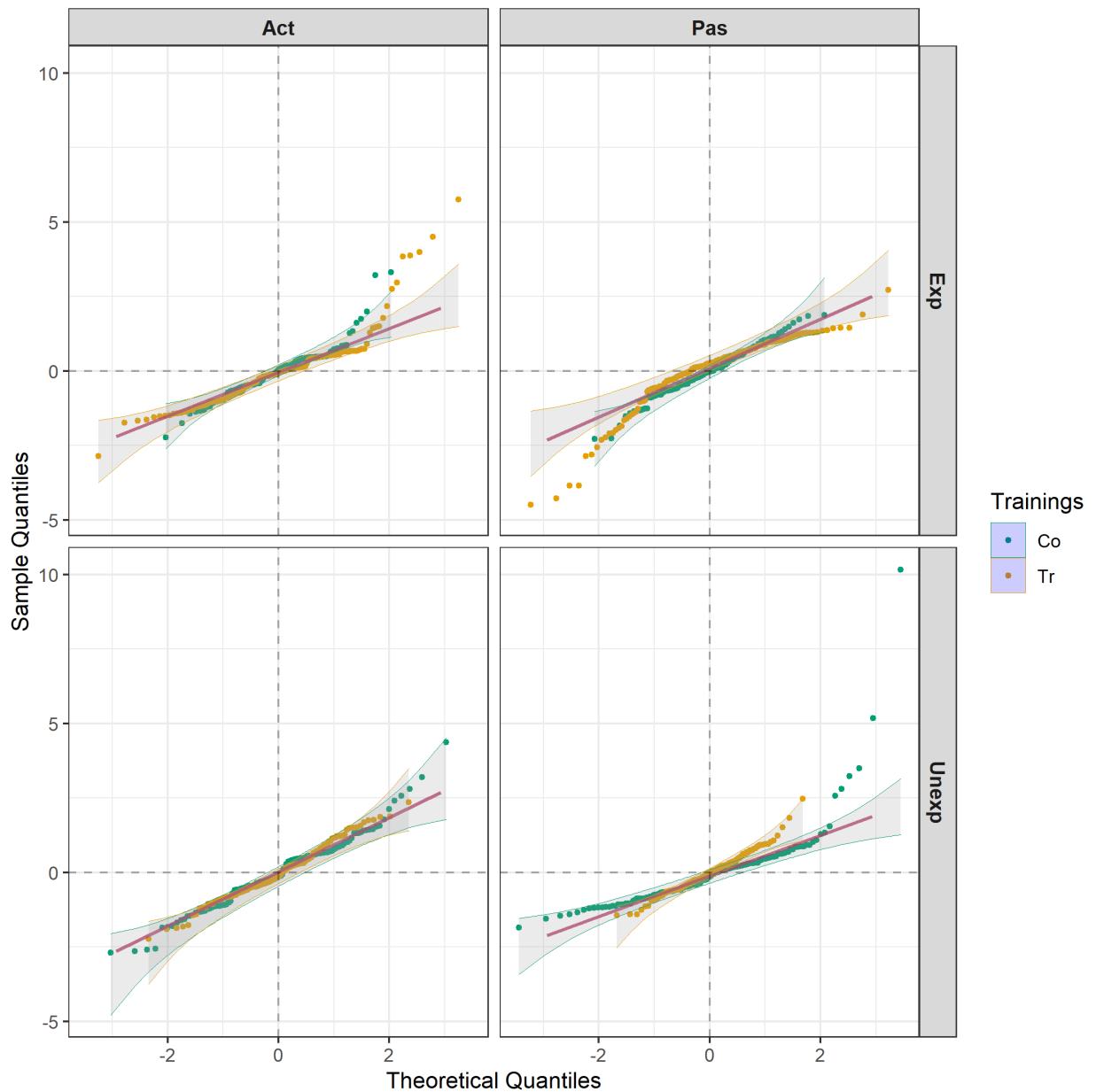


Figure 16: plot of chunk asr_mdAIC

```

(md.AIC.diffs$predictions)

##
## #### Predictions
##
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
##   calculated from model terms constructed solely from factors in
##   the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - The ignored set: Raters,Viewings,Patients
##
##
##   Trainings Motions Expressiveness predicted.value standard.error upper.halfLeastSignificant.limit
## 1       Co     Act          Exp      5.370101    2.003617      5.594396
## 2       Co     Act        Unexp     1.790563    2.002688      1.996696
## 3       Co     Pas          Exp     14.982800    2.024805     15.462046
## 4       Co     Pas        Unexp     3.057149    2.005508      3.314534
## 5       Tr     Act          Exp      5.261824    2.003617      5.486119
## 6       Tr     Act        Unexp     1.508846    2.002688      1.714979
## 7       Tr     Pas          Exp     13.407878    2.024805     13.887125
## 8       Tr     Pas        Unexp     2.705541    2.005508      2.962926
##   lower.halfLeastSignificant.limit est.status
## 1           5.145807  Estimable
## 2           1.584430  Estimable
## 3          14.503553  Estimable
## 4          2.799763  Estimable
## 5          5.037530  Estimable
## 6          1.302712  Estimable
## 7         12.928632  Estimable
## 8          2.448155  Estimable

plotPredictions(md.AIC.diffs$predictions, classify = "Trainings:Motions:Expressiveness",
                y = "predicted.value",
                error.intervals = "half", interval.annotate = FALSE,
                ggplotFuncs = list(facet_grid(cols = vars(Expressiveness, Motions)))))

plotPvalues(md.AIC.diffs, factors.per.grid = 2, show.sig = TRUE,
            title = "Prior allocation model, \nunequal variances")

```

Print out AIC values

```

(AIC.tab <- cbind(Model = letters[1:4], AIC.tab))

##   Model fixedDF varDF NBound      AIC      BIC      loglik
## 1     a        0     4      0 3041.308 3061.588 -1516.654
## 2     b        0     7      1 2291.709 2327.198 -1138.854
## 3     c        0    10      0 2965.908 3016.607 -1472.954
## 4     d        0     9      1 2283.257 2328.886 -1132.629

```

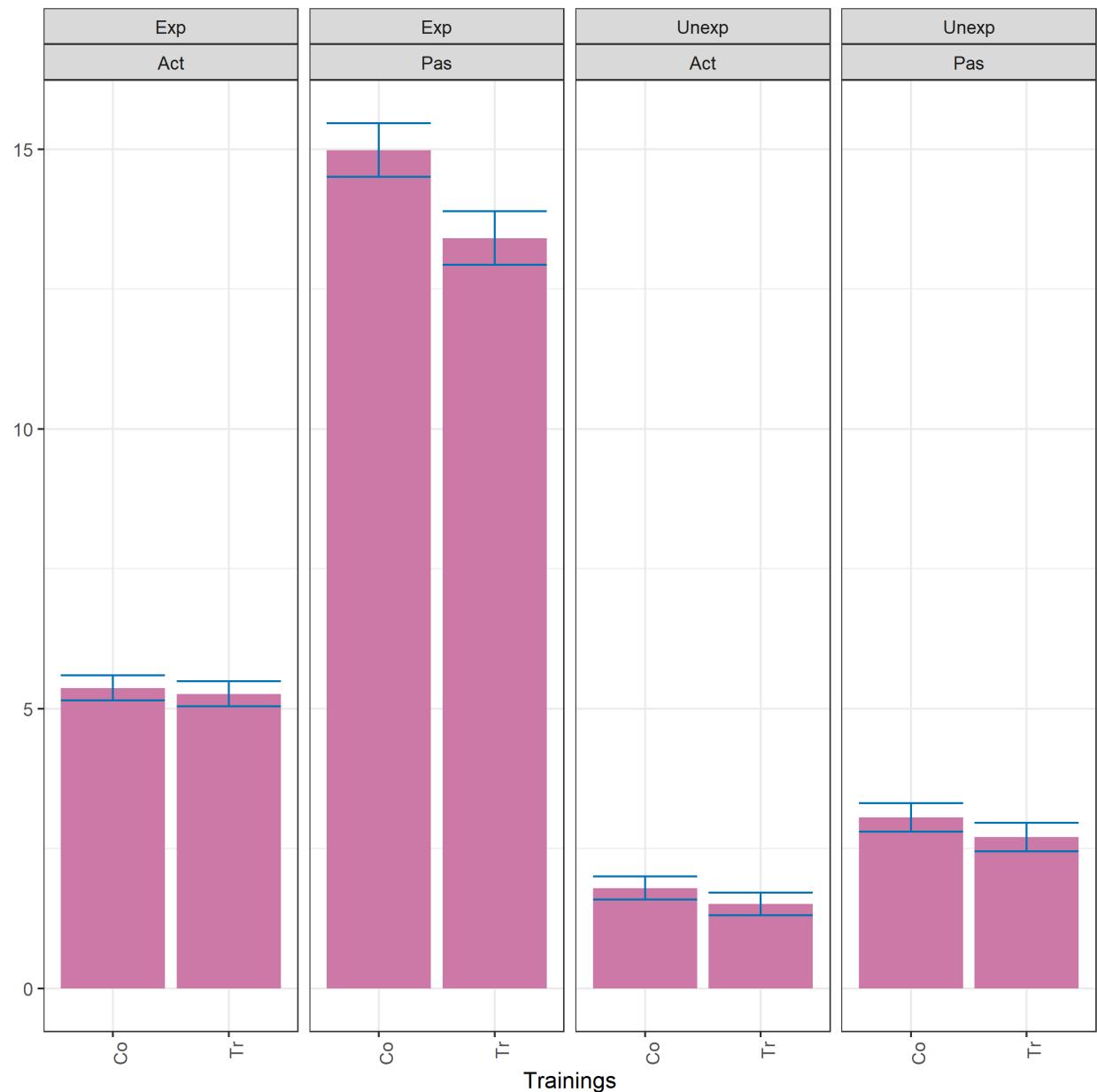


Figure 17: plot of chunk unnamed-chunk-23

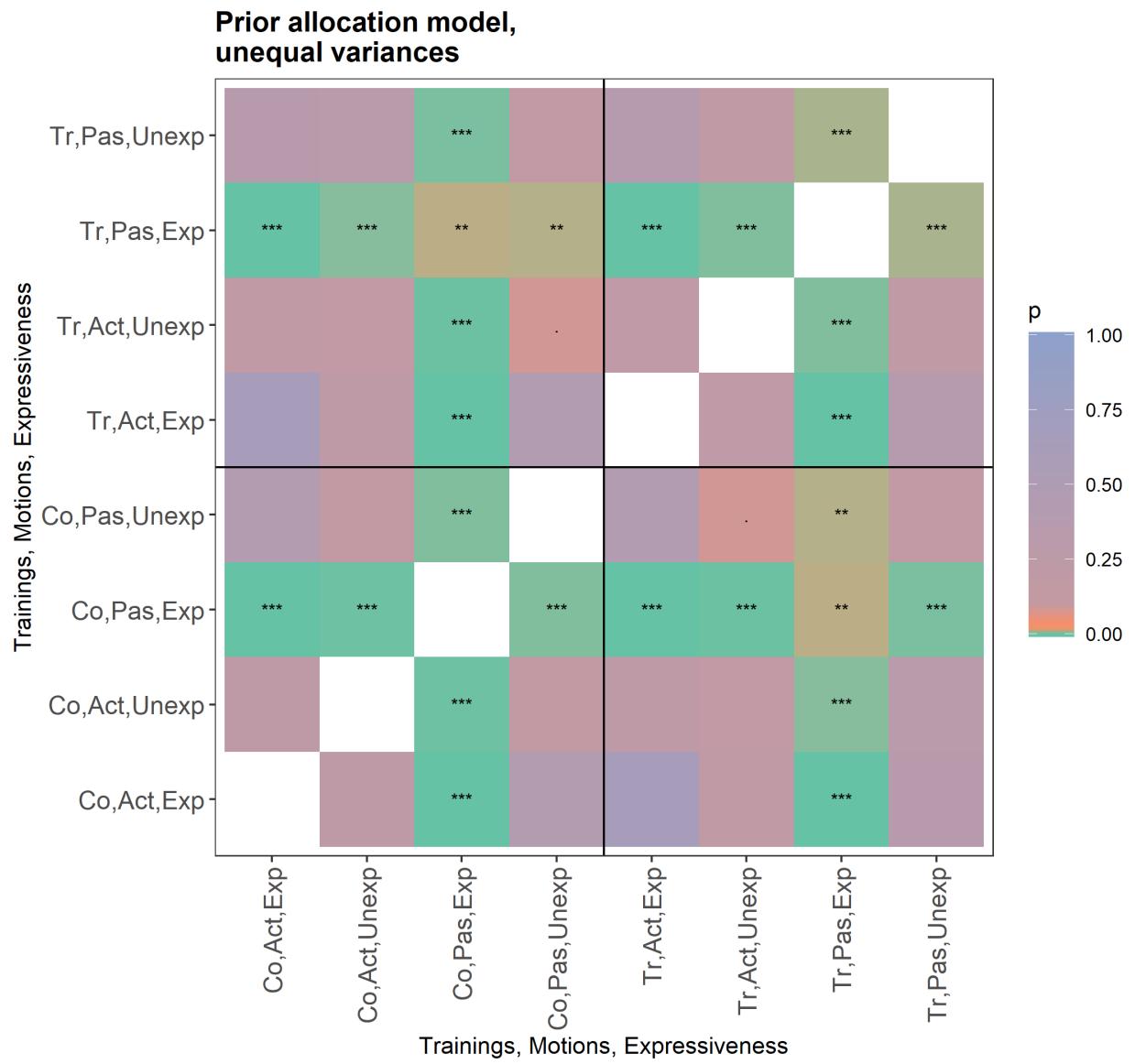


Figure 18: plot of chunk unnamed-chunk-23

Save the workspace

```
save.image("FHanal.RData")
```